

## ❖ Snapshot of Standards

- 1<sup>st</sup> Nine Weeks: Essential Questions & Academic Vocabulary
- 2<sup>nd</sup> Nine Weeks: Essential Questions & Academic Vocabulary
- 3<sup>rd</sup> Nine Weeks: Essential Questions & Academic Vocabulary
- 4<sup>th</sup> Nine Weeks: Essential Questions & Academic Vocabulary

## ❖ Unpacking Document (6<sup>th</sup> Grade) with RESOURCES

## ❖ Unpacking Document (7<sup>th</sup> Grade) with RESOURCES

### ○ Released EOG

### Math eBook

### ○ EOG Percentages and Weighted Distribution

### ○ 8 Mathematical Practices

### ○ Progression Chart

## ○ MENU of RESOURCES

### ○ Video links

### ○ Assessment Options

### ○ EOG Prep

### ○ STEM / Project Based learning links



**2017- 2018**

**Standard Division  
Document**

**Math 6<sup>+</sup>**

**Compacted-Accelerated  
Curriculum**

First Nine Weeks  
**SNAPSHOT**

Major Concepts:

- **Number Systems:** Multiplying and dividing fractions by fractions. Decimals: Multi-digit numbers, common factors and multiples. Rational numbers. **Solving real-world problems involving the four operations with rational numbers.**

Standards

- |                                |                               |
|--------------------------------|-------------------------------|
| <a href="#">6.NS.1</a>         | <a href="#">7.NS.1a,b,c,d</a> |
| <a href="#">6.NS.2</a>         | <a href="#">7.NS.2a,b,c,d</a> |
| <a href="#">6.NS.3</a>         | <a href="#">7.NS.3</a>        |
| <a href="#">6.NS.4</a>         |                               |
| <a href="#">6.NS.5</a>         |                               |
| <a href="#">6.NS.6 a,b,c</a>   |                               |
| <a href="#">6.NS.7 a,b,c,d</a> |                               |
| <a href="#">6.NS.8</a>         |                               |

Second Nine Weeks  
**SNAPSHOT**

Major Concepts:

- **Ratios and Proportional Relationships:** Use tables to compare ratios. Unit Rate. Find missing values, and plot pairs of values on coordinate plane. **Compute Unit rates**

Standards

- |                                    |                        |
|------------------------------------|------------------------|
| <a href="#">6.RP.1</a>             | <a href="#">7.RP.1</a> |
| <a href="#">6.RP.2</a>             |                        |
| <a href="#">6.RP.3, a, b, c, d</a> |                        |

Third Nine Weeks  
**SNAPSHOT**

Major Concepts:

- **Geometry:** Area, Surface area and volume. **Unique conditions that determine a triangle. Slicing three dimensional figures**
- **Statistics and Probability:** Statistical variability. **Draw numerical data from random samples for comparative inferences.**

Standards

- |                                    |                        |
|------------------------------------|------------------------|
| <a href="#">6.G.1</a>              | <a href="#">7.G.2</a>  |
| <a href="#">6.G.2</a>              | <a href="#">7.G.3</a>  |
| <a href="#">6.G.3</a>              | <a href="#">6.G.4</a>  |
| <a href="#">6.SP.1</a>             | <a href="#">7.SP.1</a> |
| <a href="#">6.SP.2</a>             | <a href="#">7.SP.2</a> |
| <a href="#">6.SP.3</a>             | <a href="#">7.SP.3</a> |
| <a href="#">6.SP.4</a>             | <a href="#">7.SP.4</a> |
| <a href="#">6.SP.5, a, b, c, d</a> |                        |

Fourth Nine Weeks  
**SNAPSHOT**

Major Concepts:

- **Expressions and Equations:** One variable equations, inequalities. Dependent and independent variables.

Standards

- |                                 |                        |
|---------------------------------|------------------------|
| <a href="#">6.EE.1</a>          | <a href="#">6.EE.4</a> |
| <a href="#">6.EE.2, a, b, c</a> | <a href="#">6.EE.6</a> |
| <a href="#">6.EE.3</a>          | <a href="#">6.EE.8</a> |
| <a href="#">6.EE.5</a>          |                        |
| <a href="#">6.EE.7</a>          |                        |
| <a href="#">6.EE.9</a>          |                        |

[Return to Main Menu](#)

**TIMELINE:** THE TIMEFRAME TO ADDRESS THE STANDARDS OF THIS COURSE ARE DEPENDANT UPON PRE-ASSESSMENTS ADMINISTERED BY INDIVIDUAL TEACHERS TO USE TO COMPACT THE CURRICULUM AS NEEDED PER EACH NINE WEEK PERIOD. THEREFORE, NO SET TIMELINE CAN BE SUGGESTED AS INSTRUCTION IS CONTINGENT UPON THE PERFORMANCE LEVELS OF CLASSES AT THEIR INDIVIDUAL SCHOOLS. HOWEVER, EDUCATORS SHOULD NOT DEVIATE FROM THE FORMATED SEQUENCE AS IT ADHERES TO THE MATHEMATICAL COHERENCE AND FLUENCY FOR THIS COURSE.



North Carolina Department of Public Instruction

## **INSTRUCTIONAL SUPPORT TOOLS**

FOR ACHIEVING NEW STANDARDS

### **6<sup>th</sup> Grade Mathematics • Unpacked Contents**

For the new Common Core standards that will be effective in all North Carolina schools in the 2012-13 School Year.

This document is designed to help North Carolina educators teach the Common Core (Standard Course of Study). NCDPI staff are continually updating and improving these tools to better serve teachers.

#### **What is the purpose of this document?**

To increase student achievement by ensuring educators understand specifically what the new standards mean a student must know, understand and be able to do.

#### **What is in the document?**

Descriptions of what each standard means a student will know, understand and be able to do. The “unpacking” of the standards done in this document is an effort to answer a simple question “What does this standard mean that a student must know and be able to do?” and to ensure the description is helpful, specific and comprehensive for educators.

#### **How do I send Feedback?**

We intend the explanations and examples in this document to be helpful and specific. That said, we believe that as this document is used, teachers and educators will find ways in which the unpacking can be improved and made ever more useful. Please send feedback to us at [feedback@dpi.state.nc.us](mailto:feedback@dpi.state.nc.us) and we will use your input to refine our unpacking of the standards. Thank You!

#### **Just want the standards alone?**

You can find the standards alone at <http://corestandards.org/the-standards>

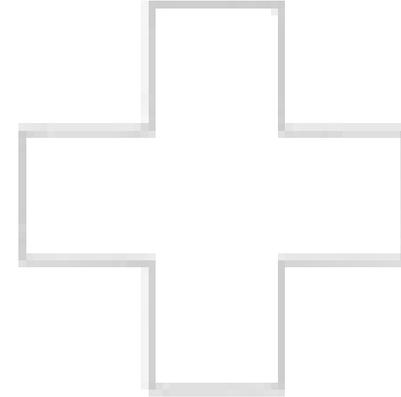
**[Return to Main Menu](#)**

## At A Glance

This page was added to give a snapshot of the mathematical concepts that are new or have been removed from this grade level as well as instructional considerations for the first year of implementation.

### New to 6<sup>th</sup> Grade:

- Unit rate (6.RP.3b)
- Measurement unit conversions (6.RP.3d)
- Number line – opposites and absolute value (6.NS.6a, 6.NS.7c)
- Vertical and horizontal distances on the coordinate plane (6.NS.8)
- Distributive property and factoring (6.EE.3)
- Introduction of independent and dependent variables (6.EE.9)
- Volume of right rectangular prisms with fractional edges (6.G.2)
- Surface area with nets (only triangle and rectangle faces) (6.G.4)
- Dot plots, histograms, box plots (6.SP.4)
- Statistical variability (Mean Absolute Deviation (MAD) and Interquartile Range (IQR)) (6.G.5c)



### Moved from 6<sup>th</sup> Grade:

- Multiplication of fractions (moved to 5<sup>th</sup> grade)
- Scientific notation (moved to 8<sup>th</sup> grade)
- Transformations (moved to 8<sup>th</sup> grade)
- Area and circumference of circles (moved to 7<sup>th</sup> grade)
- Probability (moved to 7<sup>th</sup> grade)
- Two-step equations (moved to 7<sup>th</sup> grade)
- Solving one- and two-step inequalities (moved to 7<sup>th</sup> grade)

### Notes:

- Topics may appear to be similar between the CCSS and the 2003 NCSCOS; however, the CCSS may be presented at a higher cognitive demand.
- Equivalent fractions, decimals and percents are in 6<sup>th</sup> grade but as conceptual representations (see 6.RP.2c). Use of the number line (building on elementary foundations) is also encouraged.
- For more detailed information, see the crosswalks.
- 6.NS. 2 is the final check for student understanding of place value.

### Instructional considerations for CCSS implementation in 2012 – 2013:

- Multiplication of fractions (reference 5.NF.3, 5.NF.4a, 5.NF.4b, 5.NF.5a, 5.NF.5b, 5.NF.6)
- Division of whole number by unit fractions and division of unit fractions by whole numbers (reference 5.NF.7a, 5.NF.7b, 5.NF.7c)
- Multiplication and division of decimals (reference 5.NBT.7)
- Volume with whole number (reference 5.MD.3, 5.MD.4, 5.MD.5)
- Classification of two-dimensional figures based on their properties (reference 5.G.3, 5.G.4)

[Return to Main Menu](#)

## Standards for Mathematical Practice

The Common Core State Standards for Mathematical Practice are expected to be integrated into every mathematics lesson for all students Grades K-12. Below are a few examples of how these Practices may be integrated into tasks that students complete.

Standards for Mathematical Practice	Explanations and Examples
<b>1. Make sense of problems and persevere in solving them.</b>	In grade 6, students solve real world problems through the application of algebraic and geometric concepts. These problems involve ratio, rate, area and statistics. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, “What is the most efficient way to solve the problem?”, “Does this make sense?”, and “Can I solve the problem in a different way?” Students can explain the relationships between equations, verbal descriptions, tables and graphs. Mathematically proficient students check answers to problems using a different method.
<b>2. Reason abstractly and quantitatively.</b>	In grade 6, students represent a wide variety of real world contexts through the use of real numbers and variables in mathematical expressions, equations, and inequalities. Students contextualize to understand the meaning of the number or variable as related to the problem and decontextualize to manipulate symbolic representations by applying properties of operations.
<b>3. Construct viable arguments and critique the reasoning of others.</b>	In grade 6, students construct arguments using verbal or written explanations accompanied by expressions, equations, inequalities, models, and graphs, tables, and other data displays (i.e. box plots, dot plots, histograms, etc.). They further refine their mathematical communication skills through mathematical discussions in which they critically evaluate their own thinking and the thinking of other students. They pose questions like “How did you get that?”, “Why is that true?” “Does that always work?” They explain their thinking to others and respond to others’ thinking.
<b>4. Model with mathematics.</b>	In grade 6, students model problem situations symbolically, graphically, tabularly, and contextually. Students form expressions, equations, or inequalities from real world contexts and connect symbolic and graphical representations. Students begin to explore covariance and represent two quantities simultaneously. Students use number lines to compare numbers and represent inequalities. They use measures of center and variability and data displays (i.e. box plots and histograms) to draw inferences about and make comparisons between data sets. Students need many opportunities to connect and explain the connections between the different representations. They should be able to use all of these representations as appropriate to a problem context.
<b>5. Use appropriate tools strategically.</b>	Students consider available tools (including estimation and technology) when solving a mathematical problem and decide when certain tools might be helpful. For instance, students in grade 6 may decide to represent figures on the coordinate plane to calculate area. Number lines are used to understand division and to create dot plots, histograms and box plots to visually compare the center and variability of the data. Additionally, students might use physical objects or applets to construct nets and calculate the surface area of three-dimensional figures.

[Return to Main Menu](#)

Standards for Mathematical Practice	Explanations and Examples
<b>6. Attend to precision.</b>	In grade 6, students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students use appropriate terminology when referring to rates, ratios, geometric figures, data displays, and components of expressions, equations or inequalities.
<b>7. Look for and make use of structure.</b>	Students routinely seek patterns or structures to model and solve problems. For instance, students recognize patterns that exist in ratio tables recognizing both the additive and multiplicative properties. Students apply properties to generate equivalent expressions (i.e. $6 + 2x = 2(3 + x)$ by distributive property) and solve equations (i.e. $2c + 3 = 15$ , $2c = 12$ by subtraction property of equality, $c=6$ by division property of equality). Students compose and decompose two- and three-dimensional figures to solve real world problems involving area and volume.
<b>8. Look for and express regularity in repeated reasoning.</b>	In grade 6, students use repeated reasoning to understand algorithms and make generalizations about patterns. During multiple opportunities to solve and model problems, they may notice that $a/b \div c/d = ad/bc$ and construct other examples and models that confirm their generalization. Students connect place value and their prior work with operations to understand algorithms to fluently divide multi-digit numbers and perform all operations with multi-digit decimals. Students informally begin to make connections between covariance, rates, and representations showing the relationships between quantities.

[Return to Main Menu](#)

## Grade 6 Critical Areas (from CCSS pgs. 39 – 40)

The Critical Areas are designed to bring focus to the standards at each grade by describing the big ideas that educators can use to build their curriculum and to guide instruction. The Critical Areas for sixth grade can be found beginning on page 39 in the *Common Core State Standards for Mathematics*.

1. **Connecting ratio and rate to whole number multiplication and division and using concepts of ratio and rate to solve problems.**

Students use reasoning about multiplication and division to solve ratio and rate problems about quantities. By viewing equivalent ratios and rates as deriving from, and extending, pairs of rows (or columns) in the multiplication table, and by analyzing simple drawings that indicate the relative size of quantities, students connect their understanding of multiplication and division with ratios and rates. Thus students expand the scope of problems for which they can use multiplication and division to solve problems, and they connect ratios and fractions. Students solve a wide variety of problems involving ratios and rates.

2. **Completing understanding of division of fractions and extending the notion of number to the system of rational numbers, which includes negative numbers.**

Students use the meaning of fractions, the meaning of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for dividing fractions make sense. Students use these operations to solve problems. Students extend their previous understandings of number and the ordering of numbers to the full system of rational numbers, which includes negative rational numbers, and in particular negative integers. They reason about the order and absolute value of rational numbers and about the location of points in all four quadrants of the coordinate plane.

3. **Writing, interpreting, and using expressions and equations.**

Students understand the use of variables in mathematical expressions. They write expressions and equations that correspond to given situations, evaluate expressions, and use expressions and formulas to solve problems. Students understand that expressions in different forms can be equivalent, and they use the properties of operations to rewrite expressions in equivalent forms. Students know that the solutions of an equation are the values of the variables that make the equation true. Students use properties of operations and the idea of maintaining the equality of both sides of an equation to solve simple one-step equations. Students construct and analyze tables, such as tables of quantities that are in equivalent ratios, and they use equations (such as  $3x = y$ ) to describe relationships between quantities.

4. **Developing understanding of statistical thinking.**

Building on and reinforcing their understanding of number, students begin to develop their ability to think statistically. Students recognize that a data distribution may not have a definite center and that different ways to measure center yield different values. The median measures center in the sense that it is roughly the middle value. The mean measures center in the sense that it is the value that each data point would take on if the total of the data values were redistributed equally, and also in the sense that it is a balance point. Students recognize that a measure of variability (interquartile range or mean absolute deviation) can also be useful for summarizing data because two very different sets of data can have the same mean and median yet be distinguished by their variability. Students learn to describe and summarize numerical data sets, identifying clusters, peaks, gaps, and symmetry, considering the context in which the data were collected.

5. **Reasoning about relationships among shapes to determine area, surface area, and volume.**

Students in Grade 6 also build on their work with area in elementary school by reasoning about relationships among shapes to determine area, surface area, and volume. They find areas of right triangles, other triangles, and special quadrilaterals by decomposing these shapes, rearranging or removing pieces, and relating the shapes to rectangles. Using these methods, students discuss, develop, and justify formulas for areas of triangles and parallelograms. Students find areas of polygons and surface areas of prisms and pyramids by decomposing them into pieces whose area they can determine. They reason about right rectangular prisms with fractional side lengths to extend formulas for the volume of a right rectangular prism to fractional side lengths. They prepare for work on scale drawings and constructions in Grade 7 by drawing polygons in the coordinate plane.

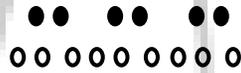
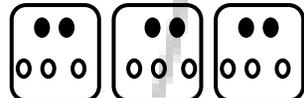
[Return to Main Menu](#)

## Common Core Cluster

### Understand ratio concepts and use ratio reasoning to solve problems.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **ratio, equivalent ratios, tape diagram, unit rate, part-to-part, part-to-whole, percent**

A detailed progression of the Ratios and Proportional Relationships domain with examples can be found at <http://commoncoretools.me/category/progressions/>

Common Core Standard	Unpacking
<p><b>Resources</b> Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. <i>For example, “The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak.” “For every vote candidate A received, candidate C received nearly three votes.”</i></p>	<p><b>6.RP.1</b> A ratio is the comparison of two quantities or measures. The comparison can be part-to-whole (ratio of guppies to all fish in an aquarium) or part-to-part (ratio of guppies to goldfish).</p> <p><u>Example 1:</u></p> <p>A comparison of 6 guppies and 9 goldfish could be expressed in any of the following forms: <math>\frac{6}{9}</math>, 6 to 9 or 6:9. If the number of guppies is represented by black circles and the number of goldfish is represented by white circles, this ratio could be modeled as</p>  <p>These values can be regrouped into 2 black circles (guppies) to 3 white circles (goldfish), which would reduce the ratio to, <math>\frac{2}{3}</math>, 2 to 3 or 2:3.</p>  <p>Students should be able to identify and describe any ratio using “For every _____, there are _____” In the example above, the ratio could be expressed saying, “For every 2 guppies, there are 3 goldfish”.</p> <p><b>NOTE:</b> Ratios are often expressed in fraction notation, although ratios and fractions do not have identical meaning. For example, ratios are often used to make “part-part” comparisons but fractions are not.</p>

**Resources** Understand the concept of a unit rate  $a/b$  associated with a ratio  $a : b$  with  $b \neq 0$ , and use rate language in the context of a ratio relationship. *For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is  $\frac{3}{4}$  cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger."*<sup>1</sup>

<sup>1</sup> Expectations for unit rates in this grade are limited to non-complex fractions.

**6.RP.2**

A unit rate expresses a ratio as part-to-one, comparing a quantity in terms of one unit of another quantity. Common unit rates are cost per item or distance per time.

Students are able to name the amount of either quantity in terms of the other quantity. Students will begin to notice that related unit rates (i.e. miles / hour and hours / mile) are reciprocals as in the second example below. At this level, students should use reasoning to find these unit rates instead of an algorithm or rule.

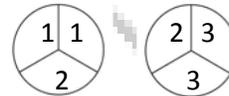
In 6<sup>th</sup> grade, students are not expected to work with unit rates expressed as complex fractions. Both the numerator and denominator of the original ratio will be whole numbers.

**Example 1:**

There are 2 cookies for 3 students. What is the amount of cookie each student would receive? (i.e. the unit rate)

*Solution:* This can be modeled as shown below to show that there is  $\frac{2}{3}$  of a cookie for 1 student, so the unit rate is

$\frac{2}{3} : 1.$

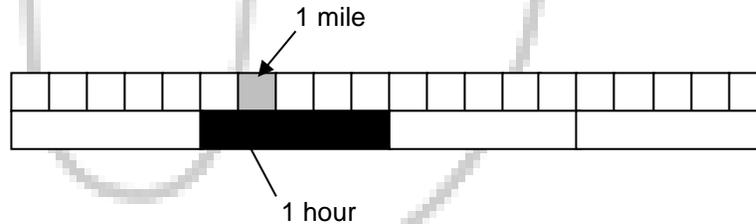


**Example 2:**

On a bicycle Jack can travel 20 miles in 4 hours. What are the unit rates in this situation, (the distance Jack can travel in 1 hour and the amount of time required to travel 1 mile)?

*Solution:* Jack can travel 5 miles in 1 hour written as  $\frac{5 \text{ mi}}{1 \text{ hr}}$  and it takes  $\frac{1}{5}$  of a hour to travel each mile written as

$\frac{1}{5} \frac{\text{hr}}{1 \text{mi}}$ . Students can represent the relationship between 20 miles and 4 hours.



[Return to Main Menu](#)

**Resources** Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.

- a. Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.

**6.RP.3** Ratios and rates can be used in ratio tables and graphs to solve problems. Previously, students have used additive reasoning in tables to solve problems. To begin the shift to proportional reasoning, students need to begin using multiplicative reasoning. Scaling up or down with multiplication maintains the equivalence. To aid in the development of proportional reasoning the cross-product algorithm is *not* expected at this level. When working with ratio tables and graphs, *whole number* measurements are the expectation for this standard.

**Example 1:**

At Books Unlimited, 3 paperback books cost \$18. What would 7 books cost? How many books could be purchased with \$54.

*Solution:* To find the price of 1 book, divide \$18 by 3. One book costs \$6. To find the price of 7 books, multiply \$6 (the cost of one book times 7 to get \$42. To find the number of books that can be purchased with \$54, multiply \$6 times 9 to get \$54 and then multiply 1 book times 9 to get 9 books. Students use ratios, unit rates and multiplicative reasoning to solve problems in various contexts, including measurement, prices, and geometry. Notice in the table below, a multiplicative relationship exists between the numbers both horizontally (times 6) and vertically (i.e.  $1 \cdot 7 = 7$ ;  $6 \cdot 7 = 42$ ). Red numbers indicate solutions.

Number of Books (n)	Cost (C)
1	6
3	18
7	42
9	54

Students use tables to compare ratios. Another bookstore offers paperback books at the prices below. Which bookstore has the best buy? Explain your answer.

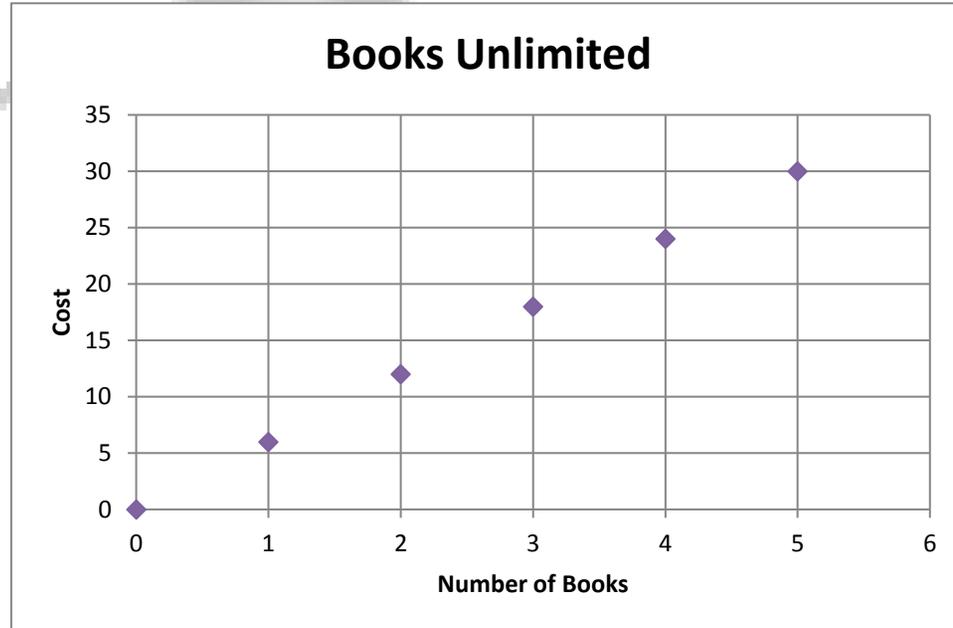
Number of Books (n)	Cost (C)
4	20
8	40

To help understand the multiplicative relationship between the number of books and cost, students write equations to express the cost of any number of books. Writing equations is foundational for work in 7<sup>th</sup> grade. For example, the equation for the first table would be  $C = 6n$ , while the equation for the second bookstore is  $C = 5n$ .

[Return to Main Menu](#)

The numbers in the table can be expressed as ordered pairs (number of books, cost) and plotted on a coordinate plane.

Students are able to plot ratios as ordered pairs. For example, a graph of Books Unlimited would be:



Example 2:

Ratios can also be used in problem solving by thinking about the total amount for each ratio unit.

The ratio of cups of orange juice concentrate to cups of water in punch is 1: 3. If James made 32 cups of punch, how many cups of orange did he need?

*Solution:* Students recognize that the total ratio would produce 4 cups of punch. To get 32 cups, the ratio would need to be duplicated 8 times, resulting in 8 cups of orange juice concentrate.

[Return to Main Menu](#)

Example 3:

Using the information in the table, find the number of yards in 24 feet.

Feet	3	6	9	15	24
Yards	1	2	3	5	?

**Solution:**

There are several strategies that students could use to determine the solution to this problem:

- Add quantities from the table to total 24 feet (9 feet and 15 feet); therefore the number of yards in 24 feet must be 8 yards (3 yards and 5 yards).
- Use multiplication to find 24 feet: 1) 3 feet x 8 = 24 feet; therefore 1 yard x 8 = 8 yards, or 2) 6 feet x 4 = 24 feet; therefore 2 yards x 4 = 8 yards.

**Example 4:**

Compare the number of black circles to white circles. If the ratio remains the same, how many black circles will there be if there are 60 white circles?



Black	4	40	20	60	?
White	3	30	15	45	60

**Solution:**

There are several strategies that students could use to determine the solution to this problem

- Add quantities from the table to total 60 white circles (15 + 45). Use the corresponding numbers to determine the number of black circles (20 + 60) to get 80 black circles.
- Use multiplication to find 60 white circles (one possibility 30 x 2). Use the corresponding numbers and operations to determine the number of black circles (40 x 2) to get 80 black circles.

b. Solve unit rate problems including those involving unit pricing and constant speed. *For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?*

Students recognize the use of ratios, unit rate and multiplication in solving problems, which could allow for the use of fractions and decimals.

**Example 1:**

In trail mix, the ratio of cups of peanuts to cups of chocolate candies is 3 to 2. How many cups of chocolate candies would be needed for 9 cups of peanuts?

[\*\*Return to Main Menu\*\*](#)

Peanuts	Chocolate
3	2

*Solution:*  
 One possible solution is for students to find the number of cups of chocolate candies for 1 cup of peanuts by dividing both sides of the table by 3, giving  $\frac{2}{3}$  cup of chocolate for each cup of peanuts. To find the amount of chocolate needed for 9 cups of peanuts, students multiply the unit rate by nine ( $9 \cdot \frac{2}{3}$ ), giving 6 cups of chocolate.

Example 2:  
 If steak costs \$2.25 per pound, how much does 0.8 pounds of steak cost? Explain how you determined your answer.

*Solution:*  
 The unit rate is \$2.25 per pound so multiply \$2.25 x 0.8 to get \$1.80 per 0.8 lb. of steak.

c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.

This is the students' first introduction to percents. Percentages are a rate per 100. Models, such as percent bars or 10 x 10 grids should be used to model percents.

Students use ratios to identify percents.

Example 1:  
 What percent is 12 out of 25?

*Solution:* One possible solution method is to set up a ratio table:  
 Multiply 25 by 4 to get 100. Multiplying 12 by 4 will give 48, meaning that 12 out of 25 is equivalent to 48 out of 100 or 48%.

Part	Whole
12	25
?	100

Students use percentages to find the part when given the percent, by recognizing that the whole is being divided into 100 parts and then taking a part of them (the percent).

Example 2:  
 What is 40% of 30?

*Solution:* There are several methods to solve this problem. One possible solution using rates is to use a 10 x 10 grid to represent the whole amount (or 30). If the 30 is divided into 100 parts, the rate for one block is 0.3. Forty percent would be 40 of the blocks, or 40 x 0.3, which equals 12.  
 See the web link below for more information.

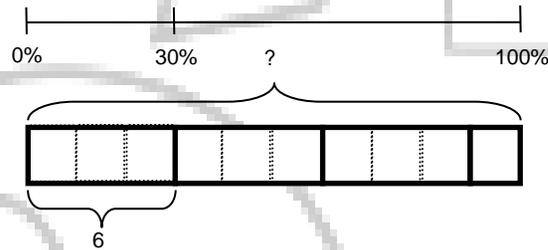
[Return to Main Menu](#)

<http://illuminations.nctm.org/LessonDetail.aspx?id=L249>

Students also determine the whole amount, given a part and the percent.

**Example 3:**

If 30% of the students in Mrs. Rutherford's class like chocolate ice cream, then how many students are in Mrs. Rutherford's class if 6 like chocolate ice cream?



(Solution: 20)

**Example 4:**

A credit card company charges 17% interest fee on any charges not paid at the end of the month. Make a ratio table to show how much the interest would be for several amounts. If the bill totals \$450 for this month, how much interest would you have to be paid on the balance?

*Solution:*

Charges	\$1	\$50	\$100	\$200	\$450
Interest	\$0.17	\$8.50	\$17	\$34	?

One possible solution is to multiply 1 by 450 to get 450 and then multiply 0.17 by 450 to get \$76.50.

- d. Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities.

A ratio can be used to compare measures of two different types, such as inches per foot, milliliters per liter and centimeters per inch. Students recognize that a conversion factor is a fraction equal to 1 since the numerator and denominator describe the same quantity. For example, 12 inches is a conversion factor since the numerator and

1 foot

denominator equal the same amount. Since the ratio is equivalent to 1, the identity property of multiplication allows an amount to be multiplied by the ratio. Also, the value of the ratio can also be expressed as 1 foot allowing for the conversion ratios to be expressed in a format so that units will “cancel”.

12 inches

[Return to Main Menu](#)

Students use ratios as conversion factors and the identity property for multiplication to convert ratio units.

Example 1:

How many centimeters are in 7 feet, given that 1 inch  $\approx$  2.54 cm?

*Solution:*

$$7 \text{ feet} \times \frac{12 \text{ inches}}{1 \text{ foot}} \times \frac{2.54 \text{ cm}}{1 \text{ inch}} = 7 \text{ feet} \times \frac{12 \text{ inches}}{1 \text{ foot}} \times \frac{2.54 \text{ cm}}{1 \text{ inch}} = 7 \times 12 \times 2.54 \text{ cm} = 213.36 \text{ cm}$$

**Note:** Conversion factors will be given. Conversions can occur both between and across the metric and English systems. Estimates are not expected.

## The Number System

6.NS

### Common Core Cluster

#### Apply and extend previous understands of multiplication and division to divide fractions by fractions.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **reciprocal, multiplicative inverses, visual fraction model**

#### Common Core Standard

#### Unpacking

What does this standard mean that a student will know and be able to do?

**Resources** Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. *For example, create a story context for  $(2/3) \div (3/4)$  and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that  $(2/3) \div (3/4) = 8/9$  because  $3/4$  of  $8/9$  is  $2/3$ . (In general,  $(a/b) \div (c/d) = ad/bc$ .) How much chocolate will each person get if 3 people share  $1/2$  lb. of chocolate equally? How many  $3/4$ -cup servings are in  $2/3$  of a cup of yogurt? How wide is a rectangular strip of land with length  $3/4$  mi and area  $1/2$  square mi?*

**6.NS.1** In 5<sup>th</sup> grade students divided whole numbers by unit fractions and divided unit fractions by whole numbers. Students continue to develop this concept by using visual models and equations to divide whole numbers by fractions and fractions by fractions to solve word problems. Students develop an understanding of the relationship between multiplication and division.

Example 1:

Students understand that a division problem such as  $3 \div \frac{2}{5}$  is asking, “how many  $\frac{2}{5}$  are in 3?” One possible visual model would begin with three whole and divide each into fifths. There are 7 groups of two-fifths in the three wholes. However, one-fifth remains. Since one-fifth is half of a two-fifths group, there is a remainder of  $\frac{1}{2}$ . Therefore,  $3 \div \frac{2}{5} = 7\frac{1}{2}$ , meaning there are  $7\frac{1}{2}$  groups of two-fifths. Students interpret the solution, explaining how division by fifths can result in an answer with halves.



This section represents one-half of two-fifths

[Return to Main Menu](#)

Students also write contextual problems for fraction division problems. For example, the problem,  $\frac{2}{3} \div \frac{1}{6}$  can be illustrated with the following word problem:

Example 2:

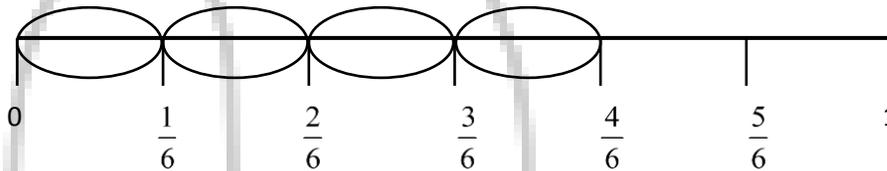
Susan has  $\frac{2}{3}$  of an hour left to make cards. It takes her about  $\frac{1}{6}$  of an hour to make each card. About how many can she make?

This problem can be modeled using a number line.

a. Start with a number line divided into thirds.



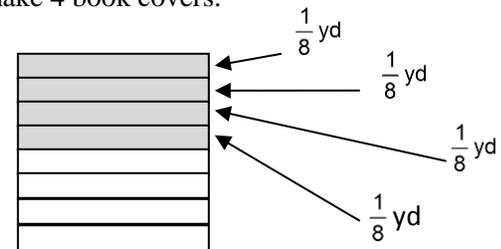
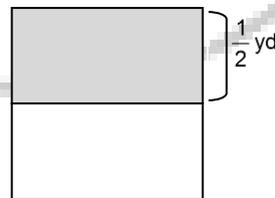
b. The problem wants to know how many sixths are in two-thirds. Divide each third in half to create sixths.



c. Each circled part represents  $\frac{1}{6}$ . There are four sixths in two-thirds; therefore, Susan can make 4 cards.

Example 3:

Michael has  $\frac{1}{2}$  of a yard of fabric to make book covers. Each book cover is made from  $\frac{1}{8}$  of a yard of fabric. How many book covers can Michael make? Solution: Michael can make 4 book covers.



**Example 4:**

Represent  $\frac{1}{2} \div \frac{2}{3}$  in a problem context and draw a model to show your solution.

**Context:** A recipe requires  $\frac{2}{3}$  of a cup of yogurt. Rachel has  $\frac{1}{2}$  of a cup of yogurt from a snack pack. How much of the recipe can Rachel make?

**Explanation of Model:**

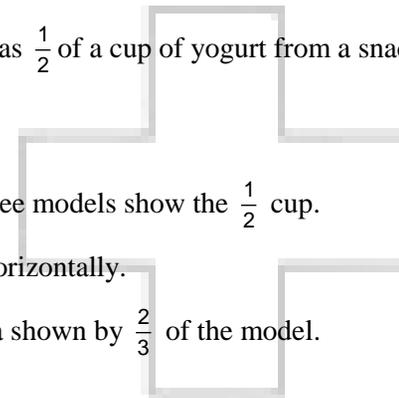
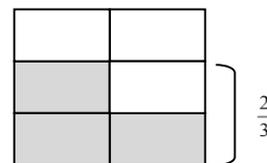
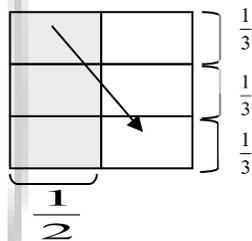
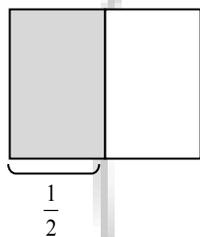
The first model shows  $\frac{1}{2}$  cup. The shaded squares in all three models show the  $\frac{1}{2}$  cup.

The second model shows  $\frac{1}{2}$  cup and also shows  $\frac{1}{3}$  cups horizontally.

The third model shows  $\frac{1}{2}$  cup moved to fit in only the area shown by  $\frac{2}{3}$  of the model.

$\frac{2}{3}$  is the new referent unit (whole).

3 out of the 4 squares in the  $\frac{2}{3}$  portion are shaded. A  $\frac{1}{2}$  cup is only  $\frac{3}{4}$  of a  $\frac{2}{3}$  cup portion, so only  $\frac{3}{4}$  of the recipe can be made.



# The Number System

6.NS

## Common Core Cluster

### Compute fluently with multi-digit numbers and find common factors and multiples.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **multi-digit**

#### Common Core Standard

#### Unpacking

What does this standard mean that a student will know and be able to do?

**Resources** Fluently divide multi-digit numbers using the standard algorithm.

**6.NS.2** In the elementary grades, students were introduced to division through concrete models and various strategies to develop an understanding of this mathematical operation (limited to 4-digit numbers divided by 2-digit numbers). In 6<sup>th</sup> grade, students become fluent in the use of the standard division algorithm, continuing to use their understanding of place value to describe what they are doing. Place value has been a major emphasis in the elementary standards. This standard is the end of this progression to address students' understanding of place value.

#### Example 1:

When dividing 32 into 8456, students should say, "there are 200 thirty-twos in 8456" as they write a 2 in the quotient. They could write 6400 beneath the 8456 rather than only writing 64.

**Resources** Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

**6.NS.3** Procedural fluency is defined by the Common Core as "skill in carrying out procedures flexibly, accurately, efficiently and appropriately". In 4<sup>th</sup> and 5<sup>th</sup> grades, students added and subtracted decimals. Multiplication and division of decimals were introduced in 5<sup>th</sup> grade (decimals to the hundredth place). At the elementary level, these operations were based on concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction. In 6<sup>th</sup> grade, students become fluent in the use of the standard algorithms of each of these operations.

The use of estimation strategies supports student understanding of decimal operations.

#### Example 1:

First estimate the sum of 12.3 and 9.75.

*Solution:* An estimate of the sum would be  $12 + 10$  or 22. Student could also state if their estimate is high or low.

Answers of 230.5 or 2.305 indicate that students are not considering place value when adding.

[Return to Main Menu](#)

## Common Core Cluster

### Compute fluently with multi-digit numbers and find common factors and multiples.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **greatest common factor, least common multiple, prime numbers, composite numbers, relatively prime, factors, multiples, distributive property, prime factorization**

#### Common Core Standard

**Resources** Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1–100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express  $36 + 8$  as  $4(9 + 2)$ .

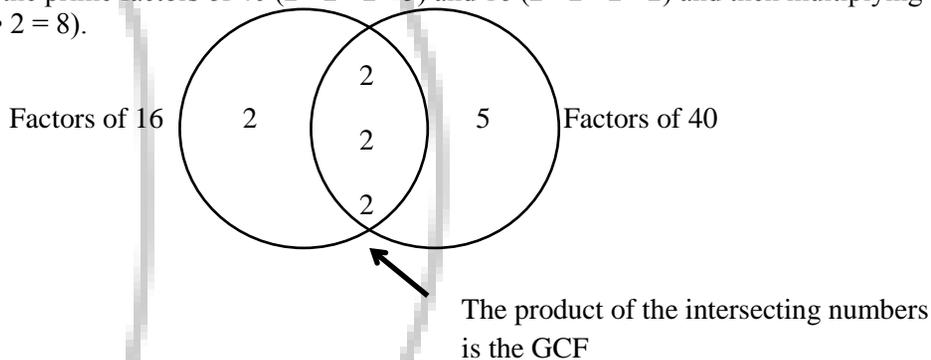
#### Unpacking

What does this standard mean that a student will know and be able to do?

**6.NS.4** In elementary school, students identified primes, composites and factor pairs (4.OA.4). In 6<sup>th</sup> grade students will find the greatest common factor of two whole numbers less than or equal to 100.

For example, the greatest common factor of 40 and 16 can be found by

- 1) listing the factors of 40 (1, 2, 4, 5, 8, 10, 20, 40) and 16 (1, 2, 4, 8, 16), then taking the greatest common factor (8). Eight (8) is also the largest number such that the other factors are **relatively prime** (two numbers with no common factors other than one). For example, 8 would be multiplied by 5 to get 40; 8 would be multiplied by 2 to get 16. Since the 5 and 2 are relatively prime, then 8 is the greatest common factor. If students think 4 is the greatest, then show that 4 would be multiplied by 10 to get 40, while 16 would be 4 times 4. Since the 10 and 4 are not relatively prime (have 2 in common), the 4 cannot be the greatest common factor.
- 2) listing the prime factors of 40 ( $2 \cdot 2 \cdot 2 \cdot 5$ ) and 16 ( $2 \cdot 2 \cdot 2 \cdot 2$ ) and then multiplying the common factors ( $2 \cdot 2 \cdot 2 = 8$ ).



Students also understand that the greatest common factor of two prime numbers is 1.

#### Example 1:

What is the greatest common factor (GCF) of 18 and 24?

*Solution:*  $2 \cdot 3^2 = 18$  and  $2^3 \cdot 3 = 24$ . Students should be able to explain that both 18 and 24 will have at least one factor of 2 and at least one factor of 3 in common, making  $2 \cdot 3$  or 6 the GCF.

[Return to Main Menu](#)

Given various pairs of addends using whole numbers from 1-100, students should be able to identify if the two numbers have a common factor. If they do, they identify the common factor and use the distributive property to rewrite the expression. They prove that they are correct by simplifying both expressions.

Example 2:

Use the greatest common factor and the distributive property to find the sum of 36 and 8.

$$36 + 8 = 4(9) + 4(2)$$

$$44 = 4(9 + 2)$$

$$44 = 4(11)$$

$$44 = 44\checkmark$$

Example 3:

Ms. Spain and Mr. France have donated a total of 90 hot dogs and 72 bags of chips for the class picnic. Each student will receive the same amount of refreshments. All refreshments must be used.

- a. What is the greatest number of students that can attend the picnic?
- b. How many bags of chips will each student receive?
- c. How many hotdogs will each student receive?

*Solution:*

- a. Eighteen (18) is the greatest number of students that can attend the picnic (GCF).
- b. Each student would receive 4 bags of chips.
- c. Each student would receive 5 hot dogs.

Students find the least common multiple of two whole numbers less than or equal to twelve. For example, the least common multiple of 6 and 8 can be found by

- 1) listing the multiplies of 6 (6, 12, 18, 24, 30, ...) and 8 (8, 26, 24, 32, 40...), then taking the least in common from the list (24); or
- 2) using the prime factorization.

Step 1: find the prime factors of 6 and 8.

$$6 = 2 \cdot 3$$

$$8 = 2 \cdot 2 \cdot 2$$

Step 2: Find the common factors between 6 and 8. In this example, the common factor is 2

Step 3: Multiply the common factors and any extra factors:  $2 \cdot 2 \cdot 2 \cdot 3$  or 24 (one of the twos is in common; the other twos and the three are the extra factors).

Example 4:

The elementary school lunch menu repeats every 20 days; the middle school lunch menu repeats every 15 days. Both schools are serving pizza today. In how many days will both schools serve pizza again?

[Return to Main Menu](#)

*Solution:* The solution to this problem will be the least common multiple (LCM) of 15 and 20. Students should be able to explain that the least common multiple is the smallest number that is a multiple of 15 and a multiple of 20. One way to find the least common multiple is to find the prime factorization of each number:  $2^2 * 5 = 20$  and  $3 * 5 = 15$ . To be a multiple of 20, a number must have 2 factors of 2 and one factor of 5 ( $2 * 2 * 5$ ). To be a multiple of 15, a number must have factors of 3 and 5. The least common multiple of 20 and 15 must have 2 factors of 2, one factor of 3 and one factor of 5 ( $2 * 2 * 3 * 5$ ) or 60.

[\*\*Return to Main Menu\*\*](#)

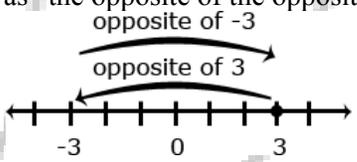
# The Number System

6.NS

## Common Core Cluster

**Apply and extend previous understandings of numbers to the system of rational numbers.**

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **rational numbers, opposites, absolute value, greater than, >, less than, <, greater than or equal to,  $\geq$ , less than or equal to,  $\leq$ , origin, quadrants, coordinate plane, ordered pairs, x-axis, y-axis, coordinates**

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<p><b>Resources</b> Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.</p>	<p><b>6.NS.5</b> Students use rational numbers (fractions, decimals, and integers) to represent real-world contexts and understand the meaning of 0 in each situation.</p> <p><b>Example 1:</b></p> <ol style="list-style-type: none"><li>Use an integer to represent 25 feet below sea level</li><li>Use an integer to represent 25 feet above sea level.</li><li>What would 0 (zero) represent in the scenario above?</li></ol> <p><b>Solution:</b></p> <ol style="list-style-type: none"><li>-25</li><li>+25</li><li>0 would represent sea level</li></ol>
<p><b>Resources</b> Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.</p> <ol style="list-style-type: none"><li>Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., <math>-(-3) = 3</math>, and that 0 is its own opposite</li></ol>	<p><b>6.NS.6</b> In elementary school, students worked with positive fractions, decimals and whole numbers on the number line and in quadrant 1 of the coordinate plane. In 6<sup>th</sup> grade, students extend the number line to represent all rational numbers and recognize that number lines may be either horizontal or vertical (i.e. thermometer) which facilitates the movement from number lines to coordinate grids. Students recognize that a number and its opposite are equidistance from zero (reflections about the zero). The opposite sign (<math>-</math>) shifts the number to the opposite side of 0. For example, <math>-4</math> could be read as “the opposite of 4” which would be negative 4. In the example, <math>-(-6.4)</math> would be read as “the opposite of the opposite of 6.4” which would be 6.4. Zero is its own opposite.</p>  <p><b>Example 1:</b></p> <p>What is the opposite of <math>2\frac{1}{2}</math>? Explain your answer?</p> <p><b>Solution:</b></p> <p><math>-2\frac{1}{2}</math> because it is the same distance from 0 on the opposite side.</p>

[Return to Main Menu](#)

- b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.
- c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.

Students worked with Quadrant I in elementary school. As the  $x$ -axis and  $y$ -axis are extending to include negatives, students begin to with the Cartesian Coordinate system. Students recognize the point where the  $x$ -axis and  $y$ -axis intersect as the origin. Students identify the four quadrants and are able to identify the quadrant for an ordered pair based on the signs of the coordinates. For example, students recognize that in Quadrant II, the signs of all ordered pairs would be  $(-, +)$ .

Students understand the relationship between two ordered pairs differing only by signs as reflections across one or both axes. For example, in the ordered pairs  $(-2, 4)$  and  $(-2, -4)$ , the  $y$ -coordinates differ only by signs, which represents a reflection across the  $x$ -axis. A change in the  $x$ -coordinates from  $(-2, 4)$  to  $(2, 4)$ , represents a reflection across the  $y$ -axis. When the signs of both coordinates change,  $[(2, -4)$  changes to  $(-2, 4)]$ , the ordered pair has been reflected across both axes.

Example 1:

Graph the following points in the correct quadrant of the coordinate plane. If the point is reflected across the  $x$ -axis, what are the coordinates of the reflected points? What similarities are between coordinates of the original point and the reflected point?

$$\left(\frac{1}{2}, -3\frac{1}{2}\right) \quad \left(-\frac{1}{2}, -3\right)$$

*Solution:*

The coordinates of the reflected points would be  $\left(\frac{1}{2}, 3\frac{1}{2}\right)$   $\left(-\frac{1}{2}, 3\right)$   $(0.25, 0.75)$ . Note that the  $y$ -coordinates are opposites.

Example 2:

Students place the following numbers would be on a number line:  $-4.5, 2, 3.2, -3\frac{3}{5}, 0.2, -2, \frac{11}{2}$ . Based on number line placement, numbers can be placed in order.

*Solution:*

The numbers in order from least to greatest are:

$$-4.5, -3\frac{3}{5}, -2, 0.2, 2, 3.2, \frac{11}{2}$$

Students place each of these numbers on a number line to justify this order.

[Return to Main Menu](#)

**Resources** Understand ordering and absolute value of rational numbers.

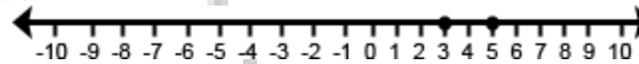
- a. Interpret statements of inequality as statements about the relative position of two numbers on a number line.  
*For example, interpret  $-3 > -7$  as a statement that  $-3$  is located to the right of  $-7$  on a number line oriented from left to right.*

**6.NS.7** Students use inequalities to express the relationship between two rational numbers, understanding that the value of numbers is smaller moving to the left on a number line.

Common models to represent and compare integers include number line models, temperature models and the profit-loss model. On a number line model, the number is represented by an arrow drawn from zero to the location of the number on the number line; the absolute value is the length of this arrow. The number line can also be viewed as a thermometer where each point of on the number line is a specific temperature. In the profit-loss model, a positive number corresponds to profit and the negative number corresponds to a loss. Each of these models is useful for examining values but can also be used in later grades when students begin to perform operations on integers. **Operations with integers are not the expectation at this level.**

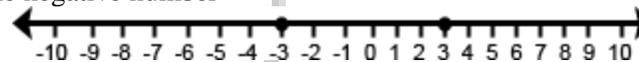
In working with number line models, students internalize the order of the numbers; larger numbers on the right (horizontal) or top (vertical) of the number line and smaller numbers to the left (horizontal) or bottom (vertical) of the number line. They use the order to correctly locate integers and other rational numbers on the number line. By placing two numbers on the same number line, they are able to write inequalities and make statements about the relationships between two numbers.

Case 1: Two positive numbers



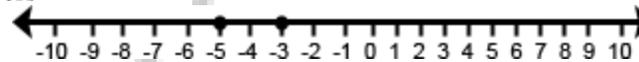
$5 > 3$   
5 is greater than 3  
3 is less than 5

Case 2: One positive and one negative number



$3 > -3$   
positive 3 is greater than negative 3  
negative 3 is less than positive 3

Case 3: Two negative numbers



$-3 > -5$   
negative 3 is greater than negative 5  
negative 5 is less than negative 3

[Return to Main Menu](#)

Example 1: Write a statement to compare  $-4\frac{1}{2}$  and  $-2$ . Explain your answer.

*Solution:*

$-4\frac{1}{2} < -2$  because  $-4\frac{1}{2}$  is located to the left of  $-2$  on the number line

Students recognize the distance from zero as the absolute value or magnitude of a rational number. Students need multiple experiences to understand the relationships between numbers, absolute value, and statements about order.

b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. *For example, write  $-3^{\circ}\text{C} > -7^{\circ}\text{C}$  to express the fact that  $-3^{\circ}\text{C}$  is warmer than  $-7^{\circ}\text{C}$ .*

Students write statements using  $<$  or  $>$  to compare rational number in context. However, explanations should reference the context rather than “less than” or “greater than”.

Example 1:

The balance in Sue’s checkbook was  $-\$12.55$ . The balance in John’s checkbook was  $-\$10.45$ . Write an inequality to show the relationship between these amounts. Who owes more?

*Solution:*  $-12.55 < -10.45$ , Sue owes more than John. The interpretation could also be “John owes less than Sue”.

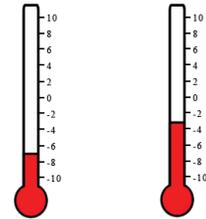
Example 2:

One of the thermometers shows  $-3^{\circ}\text{C}$  and the other shows  $-7^{\circ}\text{C}$ .

Which thermometer shows which temperature?

Which is the colder temperature? How much colder?

Write an inequality to show the relationship between the temperatures and explain how the model shows this relationship.



*Solution:*

- The thermometer on the left is  $-7$ ; right is  $-3$
- The left thermometer is colder by 4 degrees
- Either  $-7 < -3$  or  $-3 > -7$

Although 6.NS.7a is limited to two numbers, this part of the standard expands the ordering of rational numbers to more than two numbers in context.

Example 3:

A meteorologist recorded temperatures in four cities around the world. List these cities in order from coldest temperature to warmest temperature:

Albany	$5^{\circ}$
Anchorage	$-6^{\circ}$
Buffalo	$-7^{\circ}$
Juneau	$-9^{\circ}$
Reno	$12^{\circ}$

*Solution:*

[Return to Main Menu](#)

	<p>Juneau <math>-9^\circ</math>          Buffalo <math>-7^\circ</math>          Anchorage <math>-6^\circ</math>          Albany <math>5^\circ</math>          Reno <math>12^\circ</math></p>
<p>c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute as magnitude for a positive or negative quantity in a real-world situation. <i>For example, for an account balance of <math>-30</math> dollars, write <math> -30  = 30</math> to describe the size of the debt in dollars.</i></p>	<p>Students understand absolute value as the distance from zero and recognize the symbols <math>  \quad  </math> as representing absolute value.</p> <p><u>Example 1:</u>          Which numbers have an absolute value of 7  <i>Solution:</i> 7 and <math>-7</math> since both numbers have a distance of 7 units from 0 on the number line.</p> <p><u>Example 2:</u>          What is the <math> -3\frac{1}{2} </math>?  <i>Solution:</i> <math>3\frac{1}{2}</math></p> <p>In real-world contexts, the absolute value can be used to describe size or magnitude. For example, for an ocean depth of 900 feet, write <math> -900  = 900</math> to describe the distance below sea level.</p>
<p>d. Distinguish comparisons of absolute value from statements about order. <i>For example, recognize that an account balance less than <math>-30</math> dollars represents a debt greater than 30 dollars.</i></p>	<p>When working with positive numbers, the absolute value (distance from zero) of the number and the value of the number is the same; therefore, ordering is not problematic. However, negative numbers have a distinction that students need to understand. As the negative number increases (moves to the left on a number line), the value of the number decreases. For example, <math>-24</math> is less than <math>-14</math> because <math>-24</math> is located to the left of <math>-14</math> on the number line. However, absolute value is the distance from zero. In terms of absolute value (or distance) the absolute value of <math>-24</math> is greater than the absolute value of <math>-14</math>. For negative numbers, as the absolute value increases, the value of the negative number decreases.</p>
<p><b>Resources</b> Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.</p>	<p><b>6.NS.8</b> Students find the distance between points when ordered pairs have the same x-coordinate (vertical) or same y-coordinate (horizontal).</p> <p><u>Example 1:</u>          What is the distance between <math>(-5, 2)</math> and <math>(-9, 2)</math>?  <i>Solution:</i> The distance would be 4 units. This would be a horizontal line since the y-coordinates are the same. In this scenario, both coordinates are in the same quadrant. The distance can be found by using a number line to find the distance between <math>-5</math> and <math>-9</math>. Students could also recognize that <math>-5</math> is 5 units from 0 (absolute value)</p> <p style="text-align: right;"><a href="#"><b>Return to Main Menu</b></a></p>

and that  $-9$  is 9 units from 0 (absolute value). Since both of these are in the same quadrant, the distance can be found by finding the difference between the distances 9 and 5.  $(|9| - |5|)$ . Coordinates could also be in two quadrants and include rational numbers.

Example 2:

What is the distance between  $(3, -5\frac{1}{2})$  and  $(3, 2\frac{1}{4})$ ?

*Solution:* The distance between  $(3, -5\frac{1}{2})$  and  $(3, 2\frac{1}{4})$  would be  $7\frac{3}{4}$  units. This would be a vertical line since the  $x$ -coordinates are the same. The distance can be found by using a number line to count from  $-5\frac{1}{2}$  to  $2\frac{1}{4}$  or by recognizing that the distance (absolute value) from  $-5\frac{1}{2}$  to 0 is  $5\frac{1}{2}$  units and the distance (absolute value) from 0 to  $2\frac{1}{4}$  is  $2\frac{1}{4}$  units so the total distance would be  $5\frac{1}{2} + 2\frac{1}{4}$  or  $7\frac{3}{4}$  units.

Students graph coordinates for polygons and find missing vertices based on properties of triangles and quadrilaterals.

[Return to Main Menu](#)

## Expressions and Equations

6.EE

### Common Core Cluster

#### Apply and extend previous understanding of arithmetic to algebraic expressions.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **exponents, base, numerical expressions, algebraic expressions, evaluate, sum, term, product, factor, quantity, quotient, coefficient, constant, like terms, equivalent expressions, variables**

#### Common Core Standard

**Unpacking** What does this standard mean that a student will know and be able to do?

**Resources** Write and evaluate numerical expressions involving whole-number exponents.

**6.EE.1** Students demonstrate the meaning of exponents to write and evaluate numerical expressions with whole number exponents. The base can be a whole number, positive decimal or a positive fraction (i.e.  $\frac{1}{2}^5$  can be written  $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$  which has the same value as  $\frac{1}{32}$ ). Students recognize that an expression with a variable represents the same mathematics (i.e.  $x^5$  can be written as  $x \cdot x \cdot x \cdot x \cdot x$ ) and write algebraic expressions from verbal expressions.

Order of operations is introduced throughout elementary grades, including the use of grouping symbols, ( ), { }, and [ ] in 5<sup>th</sup> grade. Order of operations with exponents is the focus in 6<sup>th</sup> grade.

#### Example 1:

What is the value of:

- $0.2^3$   
*Solution:* 0.008
- $5 + 2^4 \cdot 6$   
*Solution:* 101
- $7^2 - 24 \div 3 + 26$   
*Solution:* 67

#### Example 2:

What is the area of a square with a side length of  $3x$ ?

[Return to Main Menu](#)

	<p><i>Solution:</i> <math>3x \cdot 3x = 9x^2</math></p> <p><u>Example 3:</u>  <math>4^x = 64</math>  <i>Solution:</i> <math>x = 3</math> because <math>4 \cdot 4 \cdot 4 = 64</math></p>
<p><b>Resources</b> Write, read, and evaluate expressions in which letters stand for numbers.</p> <p>a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation “Subtract y from 5” as <math>5 - y</math>.</p>	<p><b>6.EE.2</b> Students write expressions from verbal descriptions using letters and numbers, understanding order is important in writing subtraction and division problems. Students understand that the expression “5 times any number, <math>n</math>” could be represented with <math>5n</math> and that a number and letter written together means to multiply. All rational numbers may be used in writing expressions when operations are not expected. Students use appropriate mathematical language to write verbal expressions from algebraic expressions. It is <i>important</i> for students to read algebraic expressions in a manner that reinforces that the variable represents a number.</p> <p><u>Example Set 1:</u>  Students read algebraic expressions:</p> <ul style="list-style-type: none"> <li>• <math>r + 21</math> as “some number plus 21” as well as “<math>r</math> plus 21”</li> <li>• <math>n \cdot 6</math> as “some number times 6” as well as “<math>n</math> times 6”</li> <li>• <math>\frac{s}{6}</math> and <math>s \div 6</math> as “as some number divided by 6” as well as “<math>s</math> divided by 6”</li> </ul>
<p>b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. <i>For example, describe the expression <math>2(8 + 7)</math> as a product of two factors; view <math>(8 + 7)</math> as both a single entity and a sum of two terms.</i></p>	<p><u>Example Set 2:</u>  Students write algebraic expressions:</p> <ul style="list-style-type: none"> <li>• 7 less than 3 times a number  <i>Solution:</i> <math>3x - 7</math></li> <li>• 3 times the sum of a number and 5  <i>Solution:</i> <math>3(x + 5)</math></li> <li>• 7 less than the product of 2 and a number  <i>Solution:</i> <math>2x - 7</math></li> <li>• Twice the difference between a number and 5  <i>Solution:</i> <math>2(z - 5)</math></li> <li>• The quotient of the sum of <math>x</math> plus 4 and 2  <i>Solution:</i> <math>\frac{x + 4}{2}</math></li> </ul> <p>Students can describe expressions such as <math>3(2 + 6)</math> as the product of two factors: 3 and <math>(2 + 6)</math>. The quantity <math>(2 + 6)</math> is viewed as one factor consisting of two terms.</p> <p>Terms are the parts of a sum. When the term is an explicit number, it is called a constant. When the term is a product of a number and a variable, the number is called the coefficient of the variable.</p> <p style="text-align: right;"><a href="#"><b>Return to Main Menu</b></a></p>

Students should identify the parts of an algebraic expression including variables, coefficients, constants, and the names of operations (sum, difference, product, and quotient). Variables are letters that represent numbers. There are various possibilities for the number they can represent.

Consider the following expression:

$$x^2 + 5y + 3x + 6$$

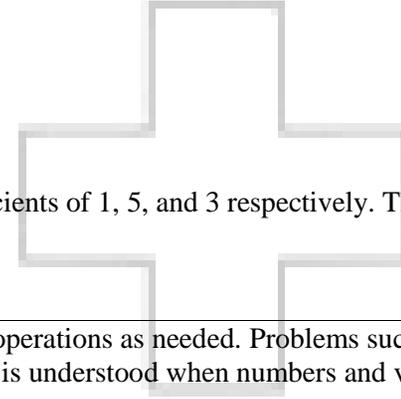
The variables are  $x$  and  $y$ .

There are 4 terms,  $x^2$ ,  $5y$ ,  $3x$ , and  $6$ .

There are 3 variable terms,  $x^2$ ,  $5y$ ,  $3x$ . They have coefficients of 1, 5, and 3 respectively. The coefficient of  $x^2$  is 1, since  $x^2 = 1x^2$ . The term  $5y$  represent  $5y$ 's or  $5 \cdot y$ .

There is one constant term,  $6$ .

The expression represents a sum of all four terms.



c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole- number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). *For example, use the formulas  $V = s^3$  and  $A = 6s^2$  to find the volume and surface area of a cube with sides of length  $s = \frac{1}{2}$ .*

Students evaluate algebraic expressions, using order of operations as needed. Problems such as example 1 below require students to understand that multiplication is understood when numbers and variables are written together and to use the order of operations to evaluate.

Order of operations is introduced throughout elementary grades, including the use of grouping symbols,  $( )$ ,  $\{ \}$ , and  $[ ]$  in 5<sup>th</sup> grade. Order of operations with exponents is the focus in 6<sup>th</sup> grade.

**Example 1:**

Evaluate the expression  $3x + 2y$  when  $x$  is equal to 4 and  $y$  is equal to 2.4.

Solution:  
 $3 \cdot 4 + 2 \cdot 2.4$   
 $12 + 4.8$   
 $16.8$

**Example 2:**

Evaluate  $5(n + 3) - 7n$ , when  $n = \frac{1}{2}$ .

Solution:

$$5\left(\frac{1}{2} + 3\right) - 7\left(\frac{1}{2}\right)$$

$$5\left(3\frac{1}{2}\right) - 3\frac{1}{2}$$

Note:  $7\left(\frac{1}{2}\right) = \frac{7}{2} = 3\frac{1}{2}$

$$17\frac{1}{2} - 3\frac{1}{2}$$

$$14$$

Students may also reason that 5 groups of  $3\frac{1}{2}$  take away 1 group of  $3\frac{1}{2}$  would give 4 groups of  $3\frac{1}{2}$ . Multiply 4 times  $3\frac{1}{2}$  to get 14.

[Return to Main Menu](#)

Example 3: Evaluate  $7xy$  when  $x = 2.5$  and  $y = 9$

*Solution:* Students recognize that two or more terms written together indicates multiplication.

$$7(2.5)(9) \\ 157.5$$

In 5<sup>th</sup> grade students worked with the grouping symbols ( ), [ ], and { }. Students understand that the fraction bar can also serve as a grouping symbol (treats numerator operations as one group and denominator operations as another group) as well as a division symbol.

Example 4:

Evaluate the following expression when  $x = 4$  and  $y = 2$

$$\frac{x^2 + y^3}{3}$$

*Solution:*

$$\frac{(4)^2 + (2)^3}{3} \quad \text{substitute the values for } x \text{ and } y$$

$$\frac{16 + 8}{3} \quad \text{raise the numbers to the powers}$$

$$\frac{24}{3} \quad \text{divide 24 by 3}$$

$$8$$

Given a context and the formula arising from the context, students could write an expression and then evaluate for any number.

Example 5:

It costs \$100 to rent the skating rink plus \$5 per person. Write an expression to find the cost for any number ( $n$ ) of people. What is the cost for 25 people?

*Solution:*

The cost for any number ( $n$ ) of people could be found by the expression,  $100 + 5n$ . To find the cost of 25 people substitute 25 in for  $n$  and solve to get  $100 + 5 * 25 = 225$ .

[Return to Main Menu](#)

Example 6:

The expression  $c + 0.07c$  can be used to find the total cost of an item with 7% sales tax, where  $c$  is the pre-tax cost of the item. Use the expression to find the total cost of an item that cost \$25.

*Solution:* Substitute 25 in for  $c$  and use order of operations to simplify

$$c + 0.07c$$

$$25 + 0.07(25)$$

$$25 + 1.75$$

$$26.75$$

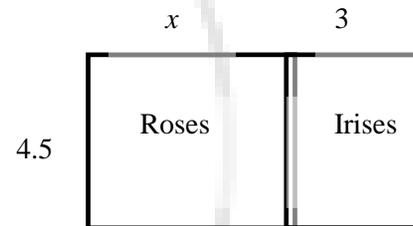
**Resources** Apply the properties of operations to generate equivalent expressions. *For example, apply the distributive property to the expression  $3(2 + x)$  to produce the equivalent expression  $6 + 3x$ ; apply the distributive property to the expression  $24x + 18y$  to produce the equivalent expression  $6(4x + 3y)$ ; apply properties of operations to  $y + y + y$  to produce the equivalent expression  $3y$ .*

**6.EE.3** Students use the distributive property to write equivalent expressions. Using their understanding of area models from elementary students illustrate the distributive property with variables.

Properties are introduced throughout elementary grades (3.OA.5); however, there has not been an emphasis on recognizing and naming the property. In 6<sup>th</sup> grade students are able to use the properties and identify by name as used when justifying solution methods (see example 4).

Example 1:

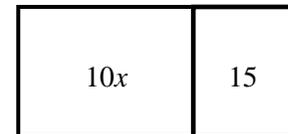
Given that the width is 4.5 units and the length can be represented by  $x + 3$ , the area of the flowers below can be expressed as  $4.5(x + 3)$  or  $4.5x + 13.5$ .



When given an expression representing area, students need to find the factors.

Example 2:

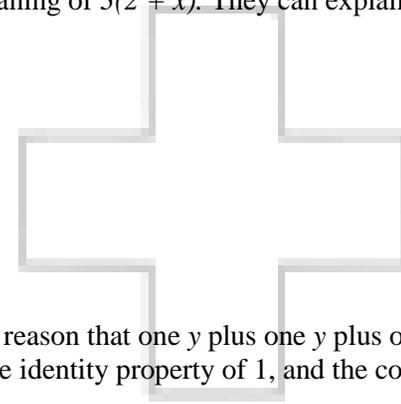
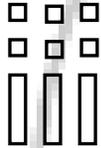
The expression  $10x + 15$  can represent the area of the figure below. Students find the greatest common factor (5) to represent the width and then use the distributive property to find the length ( $2x + 3$ ). The factors (dimensions) of this figure would be  $5(2x + 3)$ .



Example 3:

Students use their understanding of multiplication to interpret  $3(2 + x)$  as 3 groups of  $(2 + x)$ . They use a model to represent  $x$ , and make an array to show the meaning of  $3(2 + x)$ . They can explain why it makes sense that  $3(2 + x)$  is equal to  $6 + 3x$ .

An array with 3 columns and  $x + 2$  in each column:



Students interpret  $y$  as referring to one  $y$ . Thus, they can reason that one  $y$  plus one  $y$  plus one  $y$  *must be*  $3y$ . They also use the distributive property, the multiplicative identity property of 1, and the commutative property for multiplication to prove that  $y + y + y = 3y$ :

Example 4:

Prove that  $y + y + y = 3y$

*Solution:*

$$y + y + y$$

$$y \cdot 1 + y \cdot 1 + y \cdot 1$$

Multiplicative Identity

$$y \cdot (1 + 1 + 1)$$

Distributive Property

$$y \cdot 3$$

$$3y$$

Commutative Property

Example 5:

Write an equivalent expression for  $3(x + 4) + 2(x + 2)$

*Solution:*

$$3(x + 4) + 2(x + 2)$$

$$3x + 12 + 2x + 4$$

Distributive Property

$$5x + 16$$

[Return to Main Menu](#)

**Resources** Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). *For example, the expressions  $y + y + y$  and  $3y$  are equivalent because they name the same number regardless of which number  $y$  stands for.*

**6.EE.4** Students demonstrate an understanding of like terms as quantities being added or subtracted with the same variables and exponents. For example,  $3x + 4x$  are like terms and can be combined as  $7x$ ; however,  $3x + 4x^2$  are not like terms since the exponents with the  $x$  are not the same. This concept can be illustrated by substituting in a value for  $x$ . For example,  $9x - 3x = 6x$  not 6. Choosing a value for  $x$ , such as 2, can prove non-equivalence.

$$9(2) - 3(2) = 6(2)$$

however

$$9(2) - 3(2) \stackrel{?}{=} 6$$

$$18 - 6 = 12$$

$$18 - 6 \stackrel{?}{=} 6$$

$$12 = 12$$

$$12 \neq 6$$

Students can also generate equivalent expressions using the associative, commutative, and distributive properties. They can prove that the expressions are equivalent by simplifying each expression into the same form.

**Example 1:**

Are the expressions equivalent? Explain your answer?

$$4m + 8$$

$$4(m+2)$$

$$3m + 8 + m$$

$$2 + 2m + m + 6 + m$$

**Solution:**

Expression	Simplifying the Expression	Explanation
$4m + 8$	$4m + 8$	Already in simplest form
$4(m+2)$	$4(m+2)$ $4m + 8$	Distributive property
$3m + 8 + m$	$3m + 8 + m$ $3m + m + 8$ $4m + 8$	Combined like terms
$2 + 2m + m + 6 + m$	$2m + m + m + 2 + 6$ $4m + 8$	Combined like terms

[Return to Main Menu](#)

## Common Core Cluster

### Reason about and solve one-variable equations and inequalities.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **inequalities, equations, greater than, >, less than, <, greater than or equal to,  $\geq$ , less than or equal to,  $\leq$ , profit, exceed**

### Common Core Standard

**Resources** Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.

### Unpacking

What does this standard mean that a student will know and be able to do?

**6.EE.5** In elementary grades, students explored the concept of equality. In 6<sup>th</sup> grade, students explore equations as expressions being set equal to a specific value. The solution is the value of the variable that will make the equation or inequality true. Students use various processes to identify the value(s) that when substituted for the variable will make the equation true.

#### Example 1:

Joey had 26 papers in his desk. His teacher gave him some more and now he has 100. How many papers did his teacher give him?

This situation can be represented by the equation  $26 + n = 100$  where  $n$  is the number of papers the teacher gives to Joey. This equation can be stated as “some number was added to 26 and the result was 100.” Students ask themselves “What number was added to 26 to get 100?” to help them determine the value of the variable that makes the equation true. Students could use several different strategies to find a solution to the problem:

- Reasoning:  $26 + 70$  is 96 and  $96 + 4$  is 100, so the number added to 26 to get 100 is 74.
- Use knowledge of fact families to write related equations:  
 $n + 26 = 100$ ,  $100 - n = 26$ ,  $100 - 26 = n$ . Select the equation that helps to find  $n$  easily.
- Use knowledge of inverse operations: Since subtraction “undoes” addition then subtract 26 from 100 to get the numerical value of  $n$
- Scale model: There are 26 blocks on the left side of the scale and 100 blocks on the right side of the scale. All the blocks are the same size. 74 blocks need to be added to the left side of the scale to make the scale balance.
- Bar Model: Each bar represents one of the values. Students use this visual representation to demonstrate that 26 and the unknown value together make 100.

100	
26	$n$

[Return to Main Menu](#)

*Solution:*

Students recognize the value of 74 would make a true statement if substituted for the variable.

$$26 + n = 100$$

$$26 + 74 = 100$$

$$100 = 100 \checkmark$$

Example 2:

The equation  $0.44s = 11$  where  $s$  represents the number of stamps in a booklet. The booklet of stamps costs 11 dollars and each stamp costs 44 cents. How many stamps are in the booklet? Explain the strategies used to determine the answer. Show that the solution is correct using substitution.

*Solution:*

There are 25 stamps in the booklet. I got my answer by dividing 11 by 0.44 to determine how many groups of 0.44 were in 11.

By substituting 25 in for  $s$  and then multiplying, I get 11.

$$0.44(25) = 11$$

$$11 = 11 \checkmark$$

Example 3:

Twelve is less than 3 times another number can be shown by the inequality  $12 < 3n$ . What numbers could possibly make this a true statement?

*Solution:*

Since  $3 \cdot 4$  is equal to 12 I know the value must be greater than 4. Any value greater than 4 will make the inequality true. Possibilities are 4.13, 6,  $5\frac{3}{4}$ , and 200. Given a set of values, students identify the values that make the inequality true.

**Resources** Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.

**6.EE.6.** Students write expressions to represent various real-world situations.

Example Set 1:

- Write an expression to represent Susan's age in three years, when  $a$  represents her present age.
- Write an expression to represent the number of wheels,  $w$ , on any number of bicycles.
- Write an expression to represent the value of any number of quarters,  $q$ .

*Solutions:*

- $a + 3$
- $2n$
- $0.25q$

**[Return to Main Menu](#)**

Given a contextual situation, students define variables and write an expression to represent the situation.

Example 2:

The skating rink charges \$100 to reserve the place and then \$5 per person. Write an expression to represent the cost for any number of people.

$n$  = the number of people

$$100 + 5n$$

No solving is expected with this standard; however, 6.EE.2c does address the evaluating of the expressions.

Students understand the inverse relationships that can exist between two variables. For example, if Sally has 3 times as many bracelets as Jane, then Jane has  $\frac{1}{3}$  the amount of Sally. If  $S$  represents the number of bracelets Sally has, the  $\frac{1}{3}S$  or  $\frac{S}{3}$  represents the amount Jane has.

Connecting writing expressions with story problems and/or drawing pictures will give students a context for this work. It is important for students to read algebraic expressions in a manner that reinforces that the variable represents a number.

Example Set 3:

- Maria has three more than twice as many crayons as Elizabeth. Write an algebraic expression to represent the number of crayons that Maria has.  
*Solution:*  $2c + 3$  where  $c$  represents the number of crayons that Elizabeth has
- An amusement park charges \$28 to enter and \$0.35 per ticket. Write an algebraic expression to represent the total amount spent.  
*Solution:*  $28 + 0.35t$  where  $t$  represents the number of tickets purchased
- Andrew has a summer job doing yard work. He is paid \$15 per hour and a \$20 bonus when he completes the yard. He was paid \$85 for completing one yard. Write an equation to represent the amount of money he earned.  
*Solution:*  $15h + 20 = 85$  where  $h$  is the number of hours worked
- Describe a problem situation that can be solved using the equation  $2c + 3 = 15$ ; where  $c$  represents the cost of an item

[Return to Main Menu](#)

*Possible solution:*

Sarah spent \$15 at a craft store.

- She bought one notebook for \$3.
- She bought 2 paintbrushes for  $x$  dollars.

If each paintbrush cost the same amount, what was the cost of one brush?

- Bill earned \$5.00 mowing the lawn on Saturday. He earned more money on Sunday. Write an expression that shows the amount of money Bill has earned.

*Solution:*  $\$5.00 + n$

**Resources** Solve real-world and mathematical problems by writing and solving equations of the form  $x + p = q$  and  $px = q$  for cases in which  $p$ ,  $q$  and  $x$  are all nonnegative rational numbers.

**6.EE.7** Students have used algebraic expressions to generate answers given values for the variable. This understanding is now expanded to equations where the value of the variable is unknown but the outcome is known. For example, in the expression,  $x + 4$ , any value can be substituted for the  $x$  to generate a numerical answer; however, in the equation  $x + 4 = 6$ , there is only one value that can be used to get a 6. Problems should be in context when possible and use only one variable.

Students write equations from real-world problems and then use inverse operations to solve one-step equations based on real world situations. Equations may include fractions and decimals with non-negative solutions.

Students recognize that dividing by 6 and multiplying by  $\frac{1}{6}$  produces the same result. For example,  $\frac{x}{6} = 9$  and

$\frac{1}{6}x = 9$  will produce the same result.

Beginning experiences in solving equations require students to understand the meaning of the equation and the solution in the context of the problem.

Example 1:

Meagan spent \$56.58 on three pairs of jeans. If each pair of jeans costs the same amount, write an algebraic equation that represents this situation and solve to determine how much one pair of jeans cost.

\$56.58		
I	I	I

*Sample Solution:*

Students might say: "I created the bar model to show the cost of the three pairs of jeans. Each bar labeled  $J$  is the same size because each pair of jeans costs the same amount of money. The bar model represents the equation  $3J = \$56.58$ . To solve the problem, I need to divide the total cost of 56.58 between the three pairs of jeans. I know that it will be more than \$10 each because  $10 \times 3$  is only 30 but less than \$20 each because  $20 \times 3$  is 60. If I start with \$15 each, I am up to \$45. I have \$11.58 left. I then give each pair of jeans \$3. That's \$9 more dollars. I only have \$2.58 left. I continue until all the money is divided. I ended up giving each pair of jeans another \$0.86. Each pair of jeans costs \$18.86 ( $15+3+0.86$ ). I double check that the jeans cost \$18.86 each because  $\$18.86 \times 3$  is \$56.58."

[Return to Main Menu](#)

Example 2:

Julie gets paid \$20 for babysitting. He spends \$1.99 on a package of trading cards and \$6.50 on lunch. Write and solve an equation to show how much money Julie has left.

20		
1.9	6.50	money left over ( $m$ )

*Solution:*  $20 = 1.99 + 6.50 + x$ ,  $x = \$11.51$

**Resources** Write an inequality of the form  $x > c$  or  $x < c$  to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form  $x > c$  or  $x < c$  have infinitely many solutions; represent solutions of such inequalities on number line diagrams.

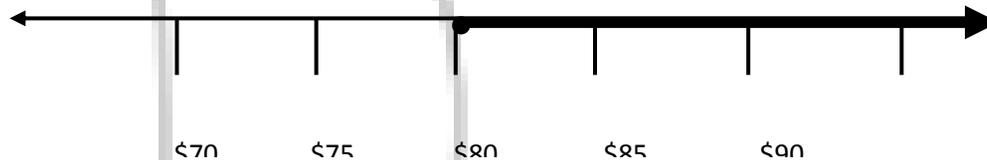
**6.EE.8** Many real-world situations are represented by inequalities. Students write inequalities to represent real world and mathematical situations. Students use the number line to represent inequalities from various contextual and mathematical situations.

Example 1:

The class must raise at least \$100 to go on the field trip. They have collected \$20. Write an inequality to represent the amount of money,  $m$ , the class still needs to raise. Represent this inequality on a number line.

*Solution:*

The inequality  $m \geq \$80$  represents this situation. Students recognize that possible values can include too many decimal values to name. Therefore, the values are represented on a number line by shading.

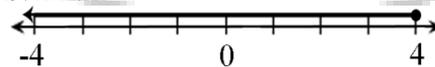


A number line diagram is drawn with an open circle when an inequality contains a  $<$  or  $>$  symbol to show solutions that are less than or greater than the number but not equal to the number. The circle is shaded, as in the example above, when the number is to be included. Students recognize that possible values can include fractions and decimals, which are represented on the number line by shading. Shading is extended through the arrow on a number line to show that an inequality has an infinite number of solutions.

Example 2:

Graph  $x \leq 4$ .

*Solution:*



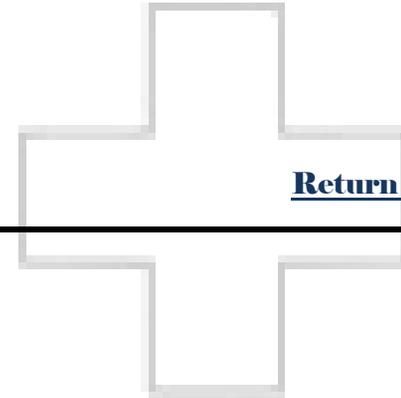
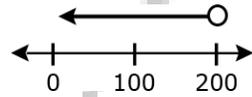
[Return to Main Menu](#)

Example 3:

The Flores family spent less than \$200.00 last month on groceries. Write an inequality to represent this amount and graph this inequality on a number line.

*Solution:*

$200 > x$ , where  $x$  is the amount spent on groceries.



[Return to Main Menu](#)

## Common Core Cluster

### Represent and analyze quantitative relationships between dependent and independent variables.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **dependent variables, independent variables, discrete data, continuous data**

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<p><b>Resources</b> Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. <i>For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation <math>d = 65t</math> to represent the relationship between distance and time.</i></p>	<p><b>6.EE.9</b> The purpose of this standard is for students to understand the relationship between two variables, which begins with the distinction between dependent and independent variables. The independent variable is the variable that can be changed; the dependent variable is the variable that is affected by the change in the independent variable. Students recognize that the independent variable is graphed on the <math>x</math>-axis; the dependent variable is graphed on the <math>y</math>-axis.</p> <p>Students recognize that not all data should be graphed with a line. Data that is discrete would be graphed with coordinates only. Discrete data is data that would not be represented with fractional parts such as people, tents, records, etc. For example, a graph illustrating the cost per person would be graphed with points since part of a person would not be considered. A line is drawn when both variables could be represented with fractional parts.</p> <p>Students are expected to recognize and explain the impact on the dependent variable when the independent variable changes (As the <math>x</math> variable increases, how does the <math>y</math> variable change?) <i>Relationships should be proportional with the line passing through the origin.</i> Additionally, students should be able to write an equation from a word problem and understand how the coefficient of the dependent variable is related to the graph and /or a table of values.</p> <p>Students can use many forms to represent relationships between quantities. Multiple representations include describing the relationship using language, a table, an equation, or a graph. Translating between multiple representations helps students understand that each form represents the same relationship and provides a different perspective.</p>

[Return to Main Menu](#)

Example 1:

What is the relationship between the two variables? Write an expression that illustrates the relationship.

$x$	1	2	3	4
$y$	2.5	5	7.5	10

*Solution:*  
 $y = 2.5x$

## Geometry

6.G

### Common Core Cluster

#### Solve real-world and mathematical problems involving area, surface area, and volume.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **area, surface area, volume, decomposing, edges, dimensions, net, vertices, face, base, height, trapezoid, isosceles, right triangle, quadrilateral, rectangles, squares, parallelograms, trapezoids, rhombi, kites, right rectangular prism, diagonal**

#### Common Core Standard

#### Unpacking

What does this standard mean that a student will know and be able to do?

**Resources** Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.

**6.G.1** Students continue to understand that area is the number of squares needed to cover a plane figure. Students should know the formulas for rectangles and triangles. “Knowing the formula” does not mean memorization of the formula. To “know” means to have an understanding of *why* the formula works and how the formula relates to the measure (area) and the figure. This understanding should be for *all* students.

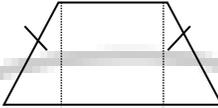
Finding the area of triangles is introduced in relationship to the area of rectangles – a rectangle can be decomposed into two congruent triangles. Therefore, the area of the triangle is  $\frac{1}{2}$  the area of the rectangle. The area of a rectangle can be found by multiplying base x height; therefore, the area of the triangle is  $\frac{1}{2}bh$  or  $(b \times h)/2$ .

The following site helps students to discover the area formula of triangles.

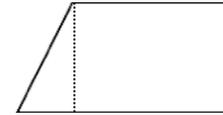
<http://illuminations.nctm.org/LessonDetail.aspx?ID=L577>

Students decompose shapes into rectangles and triangles to determine the area. For example, a trapezoid can be decomposed into triangles and rectangles (see figures below). Using the trapezoid’s dimensions, the area of the individual triangle(s) and rectangle can be found and then added together. Special quadrilaterals include rectangles, squares, parallelograms, trapezoids, rhombi, and kites.

[Return to Main Menu](#)



Isosceles trapezoid



Right trapezoid

**Note:** Students recognize the marks on the isosceles trapezoid indicating the two sides have equal measure. This is the student's first exposure to the term diagonal.

Example 1:

Find the area of a right triangle with a base length of three units, a height of four units, and a hypotenuse of 5.

*Solution:*

Students understand that the hypotenuse is the longest side of a right triangle. The base and height would form the 90° angle and would be used to find the area using:

$$A = \frac{1}{2} bh$$

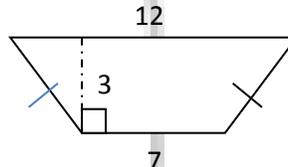
$$A = \frac{1}{2} (3 \text{ units})(4 \text{ units})$$

$$A = \frac{1}{2} 12 \text{ units}^2$$

$$A = 6 \text{ units}^2$$

Example 2:

Find the area of the trapezoid shown below using the formulas for rectangles and triangles.



*Solution:*

The trapezoid could be decomposed into a rectangle with a length of 7 units and a height of 3 units. The area of the rectangle would be 21 units<sup>2</sup>.

The triangles on each side would have the same area. The height of the triangles is 3 units. After taking away the middle rectangle's base length, there is a total of 5 units remaining for both of the side triangles. The base length of each triangle is half of 5. The base of each triangle is 2.5 units. The area of one triangle would be  $\frac{1}{2} (2.5 \text{ units})(3 \text{ units})$  or 3.75 units<sup>2</sup>.

Using this information, the area of the trapezoid would be:

$$21 \text{ units}^2$$

$$3.75 \text{ units}^2$$

$$+3.75 \text{ units}^2$$

$$28.5 \text{ units}^2$$

[Return to Main Menu](#)

Example 3:

A rectangle measures 3 inches by 4 inches. If the lengths of each side double, what is the effect on the area?

*Solution:*

The new rectangle would have side lengths of 6 inches and 8 inches. The area of the original rectangle was 12 inches<sup>2</sup>. The area of the new rectangle is 48 inches<sup>2</sup>. The area increased 4 times (quadrupled).

Students may also create a drawing to show this visually.

Example 4:

The lengths of the sides of a bulletin board are 4 feet by 3 feet. How many index cards measuring 4 inches by 6 inches would be needed to cover the board?

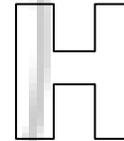
*Solution:*

Change the dimensions of the bulletin board to inches (4 feet = 48 inches; 3 feet = 36 inches). The area of the board would be 48 inches x 36 inches or 1728 inches<sup>2</sup>. The area of one index card is 24 inches<sup>2</sup>. Divide 1728 inches<sup>2</sup> by 24 inches<sup>2</sup> to get the number of index cards. 72 index cards would be needed.

Example 5:

The sixth grade class at Hernandez School is building a giant wooden H for their school. The “H” will be 10 feet tall and 10 feet wide and the thickness of the block letter will be 2.5 feet.

1. How large will the H be if measured in square feet?
2. The truck that will be used to bring the wood from the lumberyard to the school can only hold a piece of wood that is 60 inches by 60 inches. What pieces of wood (how many and which dimensions) will need to be bought to complete the project?



*Solution:*

1. One solution is to recognize that, if filled in, the area would be 10 feet tall and 10 feet wide or 100 ft<sup>2</sup>. The size of one piece removed is 5 feet by 3.75 feet or 18.75 ft<sup>2</sup>. There are two of these pieces. The area of the “H” would be 100 ft<sup>2</sup> – 18.75 ft<sup>2</sup> – 18.75 ft<sup>2</sup>, which is 62.5ft<sup>2</sup>.  
A second solution would be to decompose the “H” into two tall rectangles measuring 10 ft. by 2.5 ft. and one smaller rectangle measuring 2.5 ft. by 5 ft. The area of each tall rectangle would be 25 ft<sup>2</sup> and the area of the smaller rectangle would be 12.5 ft<sup>2</sup>. Therefore the area of the “H” would be 25 ft<sup>2</sup> + 25 ft<sup>2</sup> + 12.5 ft<sup>2</sup> or 62.5ft<sup>2</sup>.
2. Sixty inches is equal to 5 feet, so the dimensions of each piece of wood are 5ft by 5ft. Cut **two pieces of wood in half to create four pieces 5 ft. by 2.5 ft.** These pieces will make the two taller rectangles. A **third piece would be cut to measure 5ft. by 2.5 ft.** to create the middle piece.

[Return to Main Menu](#)

**Example 6:**

A border that is 2 ft. wide surrounds a rectangular flowerbed 3 ft. by 4 ft. What is the area of the border?

*Solution:*

Two sides 4 ft. by 2 ft. would be  $8\text{ft}^2 \times 2$  or  $16\text{ft}^2$

Two sides 3 ft. by 2 ft. would be  $6\text{ft}^2 \times 2$  or  $12\text{ft}^2$

Four corners measuring 2 ft. by 2 ft. would be  $4\text{ft}^2 \times 4$  or  $16\text{ft}^2$

The total area of the border would be  $16\text{ft}^2 + 12\text{ft}^2 + 16\text{ft}^2$  or  **$44\text{ft}^2$**

**Resources** Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas  $V = lwh$  and  $V = bh$  to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

**6.G.2** Previously students calculated the volume of right rectangular prisms (boxes) using whole number edges.

The use of models was emphasized as students worked to derive the formula  $V = Bh$  (5.MD.3, 5.MD.4, 5.MD.5)

The unit cube was  $1 \times 1 \times 1$ .

In 6<sup>th</sup> grade the unit cube will have fractional edge lengths. (i.e.  $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$ ) Students find the volume of the right rectangular prism with these unit cubes.

Students need multiple opportunities to measure volume by filling rectangular prisms with blocks and looking at the relationship between the total volume and the area of the base. Through these experiences, students *derive* the volume formula (volume equals the area of the base times the height). Students can explore the connection between filling a box with unit cubes and the volume formula using interactive applets such as the Cubes Tool on NCTM's Illuminations (<http://illuminations.nctm.org/ActivityDetail.aspx?ID=6>).

In addition to filling boxes, students can draw diagrams to represent fractional side lengths, connecting with multiplication of fractions. This process is similar to composing and decomposing two-dimensional shapes.

**Example 1:**

A right rectangular prism has edges of  $1\frac{1}{4}$ "",  $1$ " and  $1\frac{1}{2}$ ". How many cubes with side lengths of  $\frac{1}{4}$ " would be needed to fill the prism? What is the volume of the prism?

*Solution:*

The number of  $\frac{1}{4}$ " cubes can be found by recognizing the smaller cubes would be  $\frac{1}{4}$ " on all edges, changing the dimensions to  $\frac{5}{4}$ ",  $\frac{4}{4}$ " and  $\frac{6}{4}$ ". The number of one-fourth inch unit cubes making up the prism is 120 ( $5 \times 4 \times 6$ ).

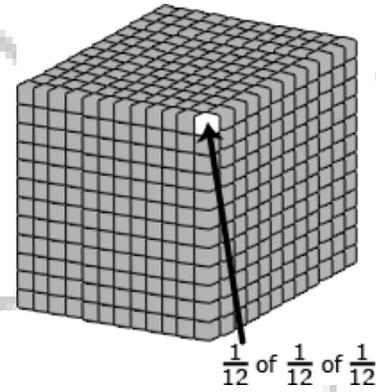
Each smaller cube has a volume of  $\frac{1}{64}$  ( $\frac{1}{4}$ " x  $\frac{1}{4}$ " x  $\frac{1}{4}$ " ), meaning 64 small cubes would make up the unit cube.

Therefore, the volume is  $\frac{5}{4} \times \frac{6}{4} \times \frac{4}{4}$  or  $\frac{120}{64}$  (120 smaller cubes with volumes of  $\frac{1}{64}$  or  $1\frac{56}{64} \rightarrow 1$  unit cube with 56 smaller cubes with a volume of  $\frac{1}{64}$ ).

**[Return to Main Menu](#)**

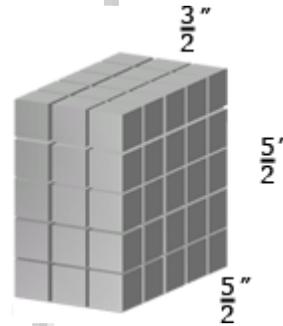
Example 2:

The model shows a cubic foot filled with cubic inches. The cubic inches can also be labeled as a fractional cubic unit with dimensions of  $\frac{1}{12}\text{ft}^3$ .



Example 3:

The model shows a rectangular prism with dimensions  $\frac{3}{2}$ ,  $\frac{5}{2}$ , and  $\frac{5}{2}$  inches. Each of the cubic units in the model is  $\frac{1}{2}$  in. on each side. Students work with the model to illustrate  $\frac{3}{2} \times \frac{5}{2} \times \frac{5}{2} = (3 \times 5 \times 5) \times \frac{1}{8}$ . Students reason that a small cube has volume of  $\frac{1}{8}$  in<sup>3</sup> because 8 of them fit in a unit cube.



[Return to Main Menu](#)

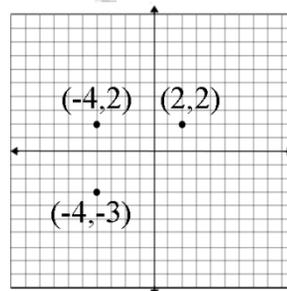
**Resources** Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.

**6.G.3** Students are given the coordinates of polygons to draw in the coordinate plane. If both  $x$ -coordinates are the same (2, -1) and (2, 4), then students recognize that a vertical line has been created and the distance between these coordinates is the distance between -1 and 4, or 5. If both the  $y$ -coordinates are the same (-5, 4) and (2, 4), then students recognize that a horizontal line has been created and the distance between these coordinates is the distance between -5 and 2, or 7. Using this understanding, student solve real-world and mathematical problems, including finding the area and perimeter of geometric figures drawn on a coordinate plane. This standard can be taught in conjunction with **6.G.1** to help students develop the formula for the triangle by using the squares of the coordinate grid. Given a triangle, students can make the corresponding square or rectangle and realize the triangle is  $\frac{1}{2}$ .

Students progress from counting the squares to making a rectangle and recognizing the triangle as  $\frac{1}{2}$  to the development of the formula for the area of a triangle.

Example 1:

If the points on the coordinate plane below are the three vertices of a rectangle, what are the coordinates of the fourth vertex? How do you know? What are the length and width of the rectangle? Find the area and the perimeter of the rectangle.



*Solution:*

To determine the distance along the  $x$ -axis between the point (-4, 2) and (2, 2) a student must recognize that -4 is  $|-4|$  or 4 units to the left of 0 and 2 is  $|2|$  or 2 units to the right of zero, so the two points are total of 6 units apart along the  $x$ -axis. Students should represent this on the coordinate grid and numerically with an absolute value expression,  $|-4| + |2|$ . The length is 6 and the width is 5.

The fourth vertex would be (2, -3).

The area would be  $5 \times 6$  or  $30 \text{ units}^2$ .

The perimeter would be  $5 + 5 + 6 + 6$  or 22 units.

[\*\*Return to Main Menu\*\*](#)

Example 2:

On a map, the library is located at  $(-2, 2)$ , the city hall building is located at  $(0,2)$ , and the high school is located at  $(0,0)$ . Represent the locations as points on a coordinate grid with a unit of 1 mile.

1. What is the distance from the library to the city hall building? The distance from the city hall building to the high school? How do you know?
2. What shape does connecting the three locations form? The city council is planning to place a city park in this area. How large is the area of the planned park?

*Solution:*

1. The distance from the library to city hall is 2 miles. The coordinates of these buildings have the same  $y$ -coordinate. The distance between the  $x$ -coordinates is 2 (from  $-2$  to  $0$ ).
2. The three locations form a right triangle. The area is  $2 \text{ mi}^2$ .

**Resources** Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.

**6.G.4** A net is a two-dimensional representation of a three-dimensional figure. Students represent three-dimensional figures whose nets are composed of rectangles and triangles. Students recognize that parallel lines on a net are congruent. Using the dimensions of the individual faces, students calculate the area of each rectangle and/or triangle and add these sums together to find the surface area of the figure.

Students construct models and nets of three-dimensional figures, describing them by the number of edges, vertices, and faces. Solids include rectangular and triangular prisms. Students are expected to use the net to calculate the surface area.

Students can create nets of 3D figures with specified dimensions using the Dynamic Paper Tool on NCTM's Illuminations (<http://illuminations.nctm.org/ActivityDetail.aspx?ID=205>).

Students also describe the types of faces needed to create a three-dimensional figure. Students make and test conjectures by determining what is needed to create a specific three-dimensional figure.

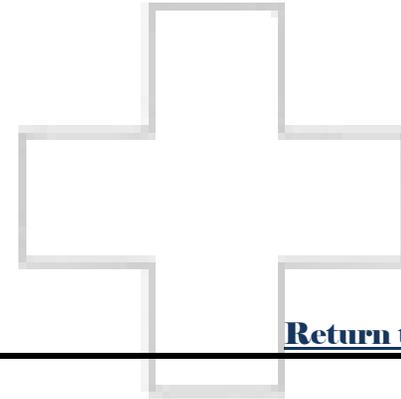
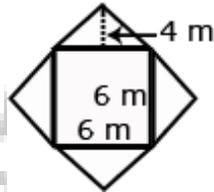
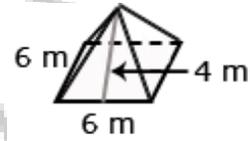
Example 1:

Describe the shapes of the faces needed to construct a rectangular pyramid. Cut out the shapes and create a model. Did your faces work? Why or why not?

**[Return to Main Menu](#)**

Example 2:

Create the net for a given prism or pyramid, and then use the net to calculate the surface area.



[Return to Main Menu](#)

## Common Core Cluster

### Develop understanding of statistical variability.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **statistics, data, variability, distribution, dot plot, histograms, box plots, median, mean**

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<p><b>Resources</b> Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. <i>For example, “How old am I?” is not a statistical question, but “How old are the students in my school?” is a statistical question because one anticipates variability in students’ ages.</i></p>	<p><b>6.SP.1</b> Statistics are numerical data relating to a group of individuals; statistics is also the name for the science of collecting, analyzing and interpreting such data. A statistical question anticipates an answer that varies from one individual to the next and is written to account for the variability in the data. Data are the numbers produced in response to a statistical question. Data are frequently collected from surveys or other sources (i.e. documents).</p> <p>Students differentiate between statistical questions and those that are not. A statistical question is one that collects information that addresses differences in a population. The question is framed so that the responses will allow for the differences. For example, the question, “How tall am I?” is not a statistical question because there is only one response; however, the question, “How tall are the students in my class?” is a statistical question since the responses anticipates variability by providing a variety of possible anticipated responses that have numerical answers. Questions can result in a narrow or wide range of numerical values.</p> <p>Students might want to know about the fitness of the students at their school. Specifically, they want to know about the exercise habits of the students. So rather than asking "Do you exercise?" they should ask about the amount of exercise the students at their school get per week. A statistical question for this study could be: “How many hours per week on average do students at Jefferson Middle School exercise?”</p>
<p><b>Resources</b> Understand that a set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</p>	<p><b>6.SP.2</b> The distribution is the arrangement of the values of a data set. Distribution can be described using center (median or mean), and spread. Data collected can be represented on graphs, which will show the shape of the distribution of the data. Students examine the distribution of a data set and discuss the center, spread and overall shape with dot plots, histograms and box plots.</p> <p><u>Example 1:</u> The dot plot shows the writing scores for a group of students on organization. Describe the data.</p> <div data-bbox="1386 1055 1680 1299" style="text-align: center;"> <p>6-Trait Writing Rubric Scores for Organization</p> </div>

[Return to Main Menu](#)

*Solution:*

The values range from 0 – 6. There is a peak at 3. The median is 3, which means 50% of the scores are greater than or equal to 3 and 50% are less than or equal to 3. The mean is 3.68. If all students scored the same, the score would be 3.68.

NOTE: Mode as a measure of center and range as a measure of variability are not addressed in the CCSS and as such are not a focus of instruction. These concepts can be introduced during instruction as needed.

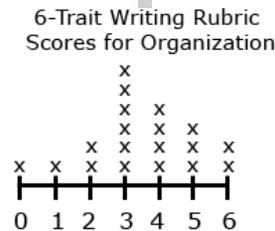
**Resources** Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

**6.SP.3** Data sets contain many numerical values that can be summarized by one number such as a measure of center. The measure of center gives a numerical value to represent the center of the data (i.e. midpoint of an ordered list or the balancing point). Another characteristic of a data set is the variability (or spread) of the values. Measures of variability are used to describe this characteristic.

Example 1:

Consider the data shown in the dot plot of the six trait scores for organization for a group of students.

- How many students are represented in the data set?
- What are the mean and median of the data set? What do these values mean? How do they compare?
- What is the range of the data? What does this value mean?



*Solution:*

- 19 students are represented in the data set.
- The mean of the data set is 3.5. The median is 3. The mean indicates that if the values were equally distributed, all students would score a 3.5. The median indicates that 50% of the students scored a 3 or higher; 50% of the students scored a 3 or lower.
- The range of the data is 6, indicating that the values vary 6 points between the lowest and highest scores.

[Return to Main Menu](#)

## Common Core Cluster

### Summarize and describe distributions.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **box plots, dot plots, histograms, frequency tables, cluster, peak, gap, mean, median, interquartile range, measures of center, measures of variability, data, Mean Absolute Deviation (M.A.D.), quartiles, lower quartile (1<sup>st</sup> quartile or  $Q_1$ ), upper quartile (3<sup>rd</sup> quartile or  $Q_3$ ), symmetrical, skewed, summary statistics, outlier**

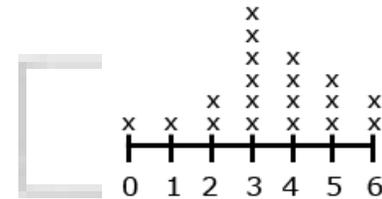
Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<p><b><u>Resources</u></b> Display numerical data in plots on a number line, including dot plots, histograms, and box plots.</p>	<p><b>6.SP.4</b> Students display data graphically using number lines. Dot plots, histograms and box plots are three graphs to be used. Students are expected to determine the appropriate graph as well as read data from graphs generated by others.</p> <p>Dot plots are simple plots on a number line where each dot represents a piece of data in the data set. Dot plots are suitable for small to moderate size data sets and are useful for highlighting the distribution of the data including clusters, gaps, and outliers.</p> <p>A histogram shows the distribution of continuous data using intervals on the number line. The height of each bar represents the number of data values in that interval. In most real data sets, there is a large amount of data and many numbers will be unique. A graph (such as a dot plot) that shows how many ones, how many twos, etc. would not be meaningful; however, a histogram can be used. Students group the data into convenient ranges and use these intervals to generate a frequency table and histogram. Note that changing the size of the bin changes the appearance of the graph and the conclusions may vary from it.</p> <p>A box plot shows the distribution of values in a data set by dividing the set into quartiles. It can be graphed either vertically or horizontally. The box plot is constructed from the five-number summary (minimum, lower quartile, median, upper quartile, and maximum). These values give a summary of the shape of a distribution. Students understand that the size of the box represents the middle 50% of the data. Statisticians have identified different methods for computing quartiles. The Standards use the method which excludes the median to create two halves. The first quartile is the median of the bottom half of the data set and the third quartile is the median of the top half of the data set. The distance between the first and third quartiles, the interquartile range (IQR), is a single number summary that serves as a useful measure of variability.</p> <p>Students can use applets to create data displays. Examples of applets include the Box Plot Tool and Histogram Tool on NCTM's Illuminations.</p> <p style="text-align: right;"><a href="#"><b><u>Return to Main Menu</u></b></a></p>

Box Plot Tool - <http://illuminations.nctm.org/ActivityDetail.aspx?ID=77>

Histogram Tool -- <http://illuminations.nctm.org/ActivityDetail.aspx?ID=78>

Example 1: Nineteen students completed a writing sample that was scored on organization. The scores for organization were 0, 1, 2, 2, 3, 3, 3, 3, 3, 3, 4, 4, 4, 4, 5, 5, 5, 6, and 6. Create a data display. What are some observations that can be made from the data display? *Solution:*

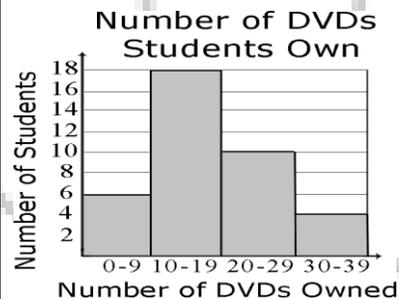
6-Trait Writing Rubric  
Scores for Organization



Example 2: Grade 6 students were collecting data for a math class project. They decided they would survey the other two grade 6 classes to determine how many DVDs each student owns. A total of 48 students were surveyed. The data are shown in the table below in no specific order. Create a data display. What are some observations that can be made from the data display?

11	21	5	12	10	31	19	13	23	33
10	11	25	14	34	15	14	29	8	5
22	26	23	12	27	4	25	15	7	
2	19	12	39	17	16	15	28	16	

*Solution:* A histogram using 5 intervals (bins) 0-9, 10-19, ...30-39) to organize the data is displayed below.



[Return to Main Menu](#)

Most of the students have between 10 and 19 DVDs as indicated by the peak on the graph. The data is pulled to the right since only a few students own more than 30 DVDs.

**Example 3:**

Ms. Wheeler asked each student in her class to write their age in months on a sticky note. The 28 students in the class brought their sticky note to the front of the room and posted them in order on the white board. The data set is listed below in order from least to greatest. Create a data display. What are some observations that can be made from the data display?

130	130	131	131	132	132	132	133	134	136
137	137	138	139	139	139	140	141	142	142
142	143	143	144	145	147	149	150		

*Solution:*

**Five number summary**

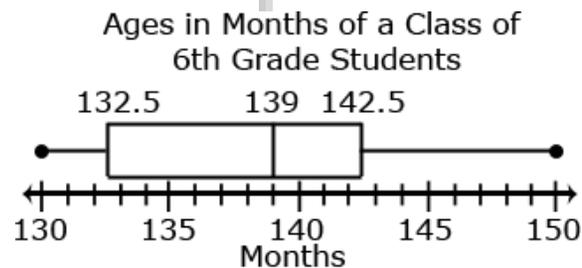
Minimum – 130 months

Quartile 1 (Q1) –  $(132 + 133) \div 2 = 132.5$  months

Median (Q2) – 139 months

Quartile 3 (Q3) –  $(142 + 143) \div 2 = 142.5$  months

Maximum – 150 months



This box plot shows that

- $\frac{1}{4}$  of the students in the class are from 130 to 132.5 months old
- $\frac{1}{4}$  of the students in the class are from 142.5 months to 150 months old
- $\frac{1}{2}$  of the class are from 132.5 to 142.5 months old
- The median class age is 139 months.

[Return to Main Menu](#)

**Resources** Summarize numerical data sets in relation to their context, such as by:

- a. Reporting the number of observations.
- b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.
- c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.
- d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.

**6.SP.5** Students summarize numerical data by providing background information about the attribute being measured, methods and unit of measurement, the context of data collection activities (addressing random sampling), the number of observations, and summary statistics. Summary statistics include quantitative measures of center (median and mean) and variability (interquartile range and mean absolute deviation) including extreme values (minimum and maximum), mean, median, mode, range, and quartiles.

Students record the number of observations. Using histograms, students determine the number of values between specified intervals. Given a box plot and the total number of data values, students identify the number of data points that are represented by the box. Reporting of the number of observations must consider the attribute of the data sets, including units (when applicable).

#### Measures of Center

Given a set of data values, students summarize the measure of center with the median or mean. The median is the value in the middle of an ordered list of data. This value means that 50% of the data is greater than or equal to it and that 50% of the data is less than or equal to it.

The mean is the arithmetic average; the sum of the values in a data set divided by how many values there are in the data set. The mean measures center in the sense that it is the value that each data point would take on if the total of the data values were redistributed equally, and also in the sense that it is a balance point.

Students develop these understandings of what the mean represents by redistributing data sets to be level or fair (equal distribution) and by observing that the total distance of the data values above the mean is equal to the total distance of the data values below the mean (balancing point).

Students use the concept of mean to solve problems. Given a data set represented in a frequency table, students calculate the mean. Students find a missing value in a data set to produce a specific average.

#### Example 1:

Susan has four 20-point projects for math class. Susan's scores on the first 3 projects are shown below:

Project 1:	18
Project 2:	15
Project 3:	16
Project 4:	??

[Return to Main Menu](#)

What does she need to make on Project 4 so that the average for the four projects is 17? Explain your reasoning.

*Solution:*

One possible solution is to calculate the total number of points needed ( $17 \times 4$  or 68) to have an average of 17. She has earned 49 points on the first 3 projects, which means she needs to earn 19 points on Project 4 ( $68 - 49 = 19$ ).

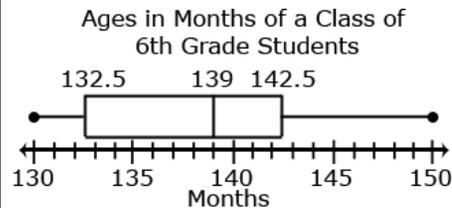
### Measures of Variability

Measures of variability/variation can be described using the interquartile range or the Mean Absolute Deviation. The interquartile range (IQR) describes the variability between the middle 50% of a data set. It is found by subtracting the lower quartile from the upper quartile. It represents the length of the box in a box plot and is not affected by outliers.

Students find the IQR from a data set by finding the upper and lower quartiles and taking the difference or from reading a box plot.

### Example 1:

What is the IQR of the data below:



*Solution:*

The first quartile is 132.5; the third quartile is 142.5. The IQR is 10 ( $142.5 - 132.5$ ). This value indicates that the values of the middle 50% of the data vary by 10.

Mean Absolute Deviation (MAD). For distributions in which the mean is the better measure of center, variation is commonly measured in terms of how far the data values deviate (distance) from the mean. Students calculate how far each value is above or below the mean, these deviations from the mean are the first step in building a measure of variation based on the spread to either side of center. Averaging the absolute values of the deviations leads to a measure of variation that is useful in characterizing the spread of a data distribution and in comparing distributions. Both the interquartile range and the Mean Absolute Deviation are represented by a single value. Students recognize that with a measure of variability, higher values represent a great variability in the data while lower values represent less variability in the data.

### Example 2:

The following data set represents the size of 9 families:

3, 2, 4, 2, 9, 8, 2, 11, 4.

What is the MAD for this data set?

[\*\*Return to Main Menu\*\*](#)

*Solution:*

The mean is 5. The MAD is the average variability of the data set. To find the MAD:

1. Find the deviation from the mean.
2. Find the absolute deviation for each of the values from step 1
3. Find the average of these absolute deviations.

The table below shows these calculations:

Data Value	Deviation from Mean	Absolute Deviation
3	-2	2
2	-3	3
4	-1	1
2	-3	3
9	4	4
8	3	3
2	-3	3
11	6	6
4	-1	1
	MAD	$26/9 = 2.89$

This value indicates that on average family size varies 2.89 from the mean of 5.

Students understand how the measures of center and measures of variability are represented by graphical displays.

Students describe the context of the data, using the shape of the data and are able to use this information to determine an appropriate measure of center and measure of variability. The measure of center that a student chooses to describe a data set will depend upon the shape of the data distribution and context of data collection. The mode is the value in the data set that occurs most frequently. The mode is the least frequently used as a measure of center because data sets may not have a mode, may have more than one mode, or the mode may not be descriptive of the data set. The mean is a very common measure of center computed by adding all the numbers in the set and dividing by the number of values.

[\*\*Return to Main Menu\*\*](#)

	<p>The mean can be affected greatly by a few data points that are very low or very high. In this case, the median or middle value of the data set might be more descriptive. In data sets that are symmetrically distributed, the mean and median will be very close to the same. In data sets that are skewed, the mean and median will be different, with the median frequently providing a better overall description of the data set.</p>
--	---

We would like to acknowledge the Arizona Department of Education for allowing us to use some of their examples and graphics.

[\*\*Return to Main Menu\*\*](#)



North Carolina Department of Public Instruction

## **INSTRUCTIONAL SUPPORT TOOLS**

FOR ACHIEVING NEW STANDARDS

### *7<sup>th</sup> Grade Mathematics* • Unpacked Content

For the new Common Core standards that will be effective in all North Carolina schools in the 2012-13 School Year.

This document is designed to help North Carolina educators teach the Common Core (Standard Course of Study). NCDPI staff are continually updating and improving these tools to better serve teachers.

#### **What is the purpose of this document?**

To increase student achievement by ensuring educators understand specifically what the new standards mean a student must know, understand and be able to do.

#### **What is in the document?**

Descriptions of what each standard means a student will know, understand and be able to do. The “unpacking” of the standards done in this document is an effort to answer a simple question “What does this standard mean that a student must know and be able to do?” and to ensure the description is helpful, specific and comprehensive for educators.

#### **How do I send Feedback?**

We intend the explanations and examples in this document to be helpful and specific. That said, we believe that as this document is used, teachers and educators will find ways in which the unpacking can be improved and made ever more useful. Please send feedback to us at [feedback@dpi.state.nc.us](mailto:feedback@dpi.state.nc.us) and we will use your input to refine our unpacking of the standards. Thank You!

#### **Just want the standards alone?**

You can find the standards alone at [www.corestandards.org](http://www.corestandards.org) .

[Return to Main Menu](#)

## At A Glance

### New to 7<sup>th</sup> Grade:

- Constant of proportionality (7.RP.2b)
- Percent of error (7.RP.3)
- Factoring to create equivalent expressions (7.EE.1)
- Triangle side lengths (7.G.2)
- Area and circumference of circles (7.G.4)
- Angles (supplementary, complementary, vertical) (7. G.5)
- Surface area and volume of pyramids (7.G.6)
- Probability (7.SP.5 – 7.SP.8)

### Moved from 7<sup>th</sup> Grade:

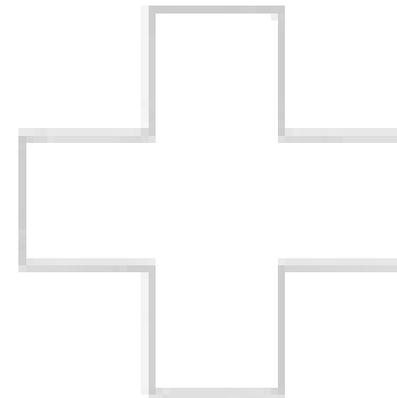
- Similar and congruent polygons (moved to 8<sup>th</sup> grade)
- Surface area and volume of cylinders (moved to 8<sup>th</sup> grade – volume only)
- Creation of box plots and histograms (moved to 6<sup>th</sup> grade – 7<sup>th</sup> grade continues to compare)
- Linear relations and functions (y-intercept moved to 8<sup>th</sup> grade)
- Views from 3-Dimensional figures (removed from CCSS)
- Statistical measures (moved to 6<sup>th</sup> grade)

### Notes:

- Topics may appear to be similar between the CCSS and the 2003 NCSCOS; however, the CCSS may be presented at a higher cognitive demand.
- Proportionality in 7<sup>th</sup> grade now includes identifying proportional relationships from tables and graphs; writing equations to represent proportional relationships.
- Using a number line for rational number operations is emphasized in CCSS.
- **For more detailed information, see the crosswalks (<http://www.ncpublicschools.org/acre/standards/common-core-tools>)**

### Instructional considerations for CCSS implementation in 2012 – 2013:

- Work with ratio tables and relationships between tables, graphs and equations; focus on the multiplicative relationship between and within ratios (6.RP.3a, 6.RP.3b)
- Unit conversions within systems (6.RP.3d)
- Opposites and absolute value (6.NS.6a, 6.NS.7c)
- Distributive property with area models and factoring (6.EE.3) – prerequisite to 7.EE.1
- Volume of rectangular prisms (6.G.2) and surface area (6.G.4) – prerequisite to 7.G.6
- Mean Absolute Deviation (6.SP.5c) – prerequisite to 7.SP.3 and foundational to standard deviation in Math One



[Return to Main Menu](#)

## Grade 7 Critical Areas (from CCSS pg. 46)

The Critical Areas are designed to bring focus to the standards at each grade by describing the big ideas that educators can use to build their curriculum and to guide instruction. The Critical Areas for seventh grade can be found on page 46 in the *Common Core State Standards for Mathematics*.

### 1. Developing understanding of and applying proportional relationships

Students extend their understanding of ratios and develop understanding of proportionality to solve single- and multi-step problems. Students use their understanding of ratios and proportionality to solve a wide variety of percent problems, including those involving discounts, interest, taxes, tips, and percent increase or decrease. Students solve problems about scale drawings by relating corresponding lengths between the objects or by using the fact that relationships of lengths within an object are preserved in similar objects. Students graph proportional relationships and understand the unit rate informally as a measure of the steepness of the related line, called the slope. They distinguish proportional relationships from other relationships.

### 2. Developing understanding of operations with rational numbers and working with expressions and linear equations

Students develop a unified understanding of number, recognizing fractions, decimals (that have a finite or a repeating decimal representation), and percents as different representations of rational numbers. Students extend addition, subtraction, multiplication, and division to all rational numbers, maintaining the properties of operations and the relationships between addition and subtraction, and multiplication and division. By applying these properties, and by viewing negative numbers in terms of everyday contexts (e.g., amounts owed or temperatures below zero), students explain and interpret the rules for adding, subtracting, multiplying, and dividing with negative numbers. They use the arithmetic of rational numbers as they formulate expressions and equations in one variable and use these equations to solve problems.

### 3. Solving problems involving scale drawings and informal geometric constructions, and working with two- and three-dimensional shapes to solve problems involving area, surface area, and volume

Students continue their work with area from Grade 6, solving problems involving the area and circumference of a circle and surface area of three-dimensional objects. In preparation for work on congruence and similarity in Grade 8 they reason about relationships among two-dimensional figures using scale drawings and informal geometric constructions, and they gain familiarity with the relationships between angles formed by intersecting lines. Students work with three-dimensional figures, relating them to two-dimensional figures by examining cross-sections. They solve real-world and mathematical problems involving area, surface area, and volume of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes and right prisms.

### 4. Drawing inferences about populations based on samples

Students build on their previous work with single data distributions to compare two data distributions and address questions about differences between populations. They begin informal work with random sampling to generate data sets and learn about the importance of representative samples for drawing inferences.

[Return to Main Menu](#)

## Ratios and Proportional Relationships

7.RP

### Common Core Cluster

**Analyze proportional relationships and use them to solve real-world and mathematical problems.**

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **unit rates, ratios, proportional relationships, proportions, constant of proportionality, complex fractions**

A detailed progression of the Ratios and Proportional Relationships domain with examples can be found at <http://commoncoretools.wordpress.com/>

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<b>RESOURCES</b> Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. <i>For example, if a person walks 1/2 mile in each 1/4 hour, compute the unit rate as the complex fraction 1/2/1/4 miles per hour, equivalently 2 miles per hour.</i>	<b>7.RP.1</b> Students continue to work with unit rates from 6 <sup>th</sup> grade; however, the comparison now includes fractions compared to fractions. The comparison can be with like or different units. Fractions may be proper or improper. <u>Example 1:</u> If $\frac{1}{2}$ gallon of paint covers $\frac{1}{6}$ of a wall, then how much paint is needed for the entire wall?  <u>Solution:</u> $\frac{1}{2}$ gal / $\frac{1}{6}$ wall.  3 gallons per 1 wall

## The Number System

7.NS

### Common Core Cluster

**Apply and extend previous understandings of operations with fractions to add, subtract, multiply, and divide rational numbers.**

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **rational numbers, integers, additive inverse**

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<b>RESOURCES</b> Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram. a. Describe situations in which opposite quantities combine to make 0. For example, a hydrogen atom has 0 charge	<b>7.NS.1</b> Students add and subtract rational numbers. Visual representations may be helpful as students begin this work; they become less necessary as students become more fluent with these operations. The expectation of the CCSS is to build on student understanding of number lines developed in 6 <sup>th</sup> grade.  <u>Example 1:</u> Use a number line to add $-5 + 7$ .

[Return to Main Menu](#)

because its two constituents are oppositely charged.

- b. Understand  $p + q$  as the number located a distance  $|q|$  from  $p$ , in the positive or negative direction depending on whether  $q$  is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.
- c. Understand subtraction of rational numbers as adding the additive inverse,  $p - q = p + (-q)$ . Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.
- d. Apply properties of operations as strategies to add and subtract rational numbers.

*Solution:*

Students find -5 on the number line and move 7 in a positive direction (to the right). The stopping point of 2 is the sum of this expression. Students also add negative fractions and decimals and interpret solutions in given contexts.

In 6<sup>th</sup> grade, students found the distance of horizontal and vertical segments on the coordinate plane. In 7<sup>th</sup> grade, students build on this understanding to recognize subtraction is finding the distance between two numbers on a number line.

In the example,  $7 - 5$ , the difference is the distance between 7 and 5, or 2, in the direction of 5 to 7 (positive). Therefore the answer would be 2.

Example 2:

Use a number line to subtract:  $-6 - (-4)$

*Solution:*

This problem is asking for the distance between -6 and -4. The distance between -6 and -4 is 2 and the direction from -4 to -6 is left or negative. The answer would be -2. Note that this answer is the same as adding the opposite of -4:  $-6 + 4 = -2$

Example 3:

Use a number line to illustrate:

- $p - q$             *ie.*  $7 - 4$
- $p + (-q)$         *ie.*  $7 + (-4)$
- Is this equation true  $p - q = p + (-q)$ ?

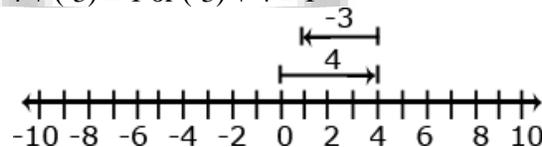
Students explore the above relationship when  $p$  is negative and  $q$  is positive and when both  $p$  and  $q$  are negative. Is this relationship always true?

Example 4:

Morgan has \$4 and she needs to pay a friend \$3. How much will Morgan have after paying her friend?

*Solution:*

$4 + (-3) = 1$  or  $(-3) + 4 = 1$



[Return to Main Menu](#)

**RESOURCES** Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.

- Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as  $(-1)(-1) = 1$  and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.
- Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If  $p$  and  $q$  are integers, then  $-(p/q) = (-p)/q = p/(-q)$ . Interpret quotients of rational numbers by describing real-world contexts.
- Apply properties of operations as strategies to multiply and divide rational numbers.
- Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats.

**7.NS.2** Students understand that multiplication and division of integers is an extension of multiplication and division of whole numbers. Students recognize that when division of rational numbers is represented with a fraction bar, each number can have a negative sign.

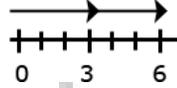
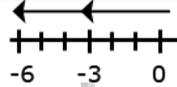
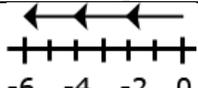
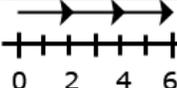
**Example 1:**

Which of the following fractions is equivalent to  $\frac{-4}{5}$ ? Explain your reasoning.

- a.  $\frac{4}{-5}$       b.  $\frac{-16}{20}$       c.  $\frac{-4}{-5}$

**Example Set 2:**

Examine the family of equations in the table below. What patterns are evident? Create a model and context for each of the products. Write and model the family of equations related to  $3 \times 4 = 12$ .

Equation	Number Line Model	Context
$2 \cdot 3 = 6$		Selling two packages of apples at \$3.00 per pack
$2 \cdot -3 = -6$		Spending 3 dollars each on 2 packages of apples
$-2 \cdot 3 = -6$		Owing 2 dollars to each of your three friends
$-2 \cdot -3 = 6$		Forgiving 3 debts of \$2.00 each

Using long division from elementary school, students understand the difference between terminating and repeating decimals. This understanding is foundational for the work with rational and irrational numbers in 8<sup>th</sup> grade.

[Return to Main Menu](#)

	<p><u>Example 3:</u> Using long division, express the following fractions as decimals. Which of the following fractions will result in terminating decimals; which will result in repeating decimals?</p> <p>Identify which fractions will terminate (the denominator of the fraction in reduced form only has factors of 2 and/or 5)</p>
<p><b><u>RESOURCES</u></b> Solve real-world and mathematical problems involving the four operations with rational numbers.<sup>1</sup></p> <p><sup>1</sup>Computations with rational numbers extend the rules for manipulating fractions to complex fractions.</p>	<p><b><u>7.NS.3</u></b> Students use order of operations from 6<sup>th</sup> grade to write and solve problem with all rational numbers.</p> <p><u>Example 1:</u> Calculate: <math>[-10(-0.9)] - [(-10) \cdot 0.11]</math></p> <p><i>Solution:</i> 10.1</p> <p><u>Example 2: (Updated)</u> Jim's cell phone bill company is automatically deducting \$32 from his bank account every month. How much will the cell phone bill deductions affect this bank account over a year?</p> <p><i>Solution:</i> <math>-32 + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) + (-32) = 12(-32)</math></p> <p><u>Example 3:</u> It took a submarine 20 seconds to drop to 100 feet below sea level from the surface. What was the rate of the descent?</p> <p><i>Solution:</i> <math>\frac{-100 \text{ feet}}{20 \text{ seconds}} = \frac{-5 \text{ feet}}{1 \text{ second}} = -5 \text{ ft/sec}</math></p> <p><u>Example 4:</u> A newspaper reports these changes in the price of a stock over four days: <math>\frac{-1}{8}, \frac{-5}{8}, \frac{3}{8}, \frac{-9}{8}</math>. What is the average daily change?</p> <p><i>Solution:</i> The sum is <math>\frac{-12}{8}</math>; dividing by 4 will give a daily average of <math>\frac{-3}{8}</math></p> <p style="text-align: right;"><a href="#">Return to Main Menu</a></p>

## Common Core Cluster

### Draw, construct, and describe geometrical figures and describe the relationships between them.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **scale drawing, dimensions, scale factor, plane sections, right rectangular prism, right rectangular pyramids, parallel, perpendicular, scalene triangle, obtuse triangle, equilateral triangle, right triangle**

**RESOURCES** Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.

**7.G.2** Students draw geometric shapes with given parameters. Parameters could include parallel lines, angles, perpendicular lines, line segments, etc.

Example 1:

Draw a quadrilateral with one set of parallel sides and no right angles.

Students understand the characteristics of angles and side lengths that create a unique triangle, more than one triangle or no triangle.

Example 2:

Can a triangle have more than one obtuse angle? Explain your reasoning.

Example 3:

Will three sides of any length create a triangle? Explain how you know which will work.

Possibilities to examine are:

- a. 13 cm, 5 cm, and 6 cm
- b. 3 cm, 3cm, and 3 cm
- c. 2 cm, 7 cm, 6 cm

*Solution:*

“A” above will not work; “B” and “C” will work. Students recognize that the sum of the two smaller sides must be larger than the third side.

Example 4:

Is it possible to draw a triangle with a 90° angle and one leg that is 4 inches long and one leg that is 3 inches long?

If so, draw one. Is there more than one such triangle?

(NOTE: Pythagorean Theorem is NOT expected – this is an exploration activity only)

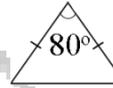
Example 5:

Draw a triangle with angles that are 60 degrees. Is this a unique triangle? Why or why not?

[Return to Main Menu](#)

Example 6:

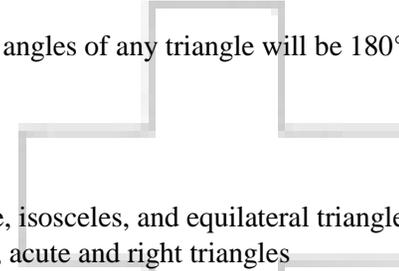
Draw an isosceles triangle with only one  $80^\circ$  angle. Is this the only possibility or can another triangle be drawn that will meet these conditions?



Through exploration, students recognize that the sum of the angles of any triangle will be  $180^\circ$  and the angles of any quadrilateral will sum to  $360^\circ$

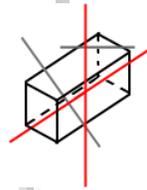
Other explorations would include:

- Base angles of an isosceles triangle are equal
- Angle and side length relationships between scalene, isosceles, and equilateral triangles
- Angle and side length relationships between obtuse, acute and right triangles



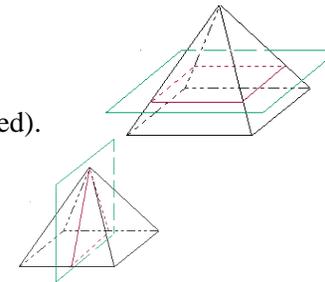
**RESOURCES** Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids.

**7.G.3** Students need to describe the resulting face shape from cuts made parallel and perpendicular to the bases of right rectangular prisms and pyramids. Cuts made parallel will take the shape of the base; cuts made perpendicular will take the shape of the lateral (side) face. Cuts made at an angle through the right rectangular prism will produce a parallelogram;



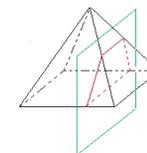
If the pyramid is cut with a plane (green) parallel to the base, the intersection of the pyramid and the plane is a square cross section (red).

If the pyramid is cut with a plane (green) passing through the top vertex and perpendicular to the base, the intersection of the pyramid and the plane is a triangular cross section (red).



If the pyramid is cut with a plane (green) perpendicular to the base, but not through the top vertex, the intersection of the pyramid and the plane is a trapezoidal cross section (red).

<http://intermath.coe.uga.edu/dictionary/descript.asp?termID=95>



[Return to Main Menu](#)

## Common Core Cluster

### Use random sampling to draw inferences about a population.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **random sampling, population, representative sample, inferences**

#### Common Core Standard

#### Unpacking

What does this standard mean that a student will know and be able to do?

**RESOURCES** Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid inferences.

**7.SP.1** Students recognize that it is difficult to gather statistics on an entire population. Instead a random sample can be representative of the total population and will generate valid predictions. Students use this information to draw inferences from data. A random sample **must** be used in conjunction with the population to get accuracy. For example, a random sample of elementary students cannot be used to give a survey about the prom.

#### Example 1:

The school food service wants to increase the number of students who eat hot lunch in the cafeteria. The student council has been asked to conduct a survey of the student body to determine the students' preferences for hot lunch. They have determined two ways to do the survey. The two methods are listed below. Determine if each survey option would produce a random sample. Which survey option should the student council use and why?

1. Write all of the students' names on cards and pull them out in a draw to determine who will complete the survey.
2. Survey the first 20 students that enter the lunchroom.
3. Survey every 3<sup>rd</sup> student who gets off a bus.

**RESOURCES** Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions. *For example, estimate the mean word length in a book by randomly sampling words from the book; predict the winner of a school election based on randomly sampled survey data. Gauge how far off the estimate or prediction might be.*

**7.SP.2** Students collect and use multiple samples of data to make generalizations about a population. Issues of variation in the samples should be addressed.

#### Example 1:

Below is the data collected from two random samples of 100 students regarding student's school lunch preference. Make at least two inferences based on the results.

Student Sample	Hamburgers	Tacos	Pizza	Total
#1	12	14	74	100
#2	12	11	77	100

#### Solution:

- Most students prefer pizza.
- More people prefer pizza and hamburgers and tacos combined.

[Return to Main Menu](#)

## Common Core Cluster

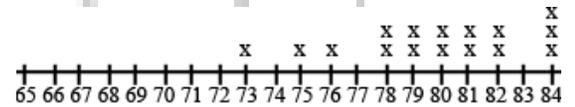
### Draw informal comparative inferences about two populations.

Mathematically proficient students communicate precisely by engaging in discussion about their reasoning using appropriate mathematical language. The terms students should learn to use with increasing precision with this cluster are: **variation/variability, distribution, measures of center, measures of variability**

Common Core Standard	Unpacking What does this standard mean that a student will know and be able to do?
<p><b>RESOURCES</b> Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability. <i>For example, the mean height of players on the basketball team is 10 cm greater than the mean height of players on the soccer team, about twice the variability (mean absolute deviation) on either team; on a dot plot, the separation between the two distributions of heights is noticeable.</i></p>	<p><b>7.SP.3</b> This is the students' first experience with comparing two data sets. Students build on their understanding of graphs, mean, median, Mean Absolute Deviation (MAD) and interquartile range from 6<sup>th</sup> grade. Students understand that</p> <ol style="list-style-type: none"> <li>1. a full understanding of the data requires consideration of the measures of variability as well as mean or median,</li> <li>2. variability is responsible for the overlap of two data sets and that an increase in variability can increase the overlap, and</li> <li>3. median is paired with the interquartile range and mean is paired with the mean absolute deviation .</li> </ol> <p><u>Example:</u> Jason wanted to compare the mean height of the players on his favorite basketball and soccer teams. He thinks the mean height of the players on the basketball team will be greater but doesn't know how much greater. He also wonders if the variability of heights of the athletes is related to the sport they play. He thinks that there will be a greater variability in the heights of soccer players as compared to basketball players. He used the rosters and player statistics from the team websites to generate the following lists.</p> <p>Basketball Team – Height of Players in inches for 2010 Season 75, 73, 76, 78, 79, 78, 79, 81, 80, 82, 81, 84, 82, 84, 80, 84</p> <p>Soccer Team – Height of Players in inches for 2010 73, 73, 73, 72, 69, 76, 72, 73, 74, 70, 65, 71, 74, 76, 70, 72, 71, 74, 71, 74, 73, 67, 70, 72, 69, 78, 73, 76, 69</p> <p>To compare the data sets, Jason creates a two dot plots on the same scale. The shortest player is 65 inches and the tallest players are 84 inches.</p> <p style="text-align: right;"><a href="#">Return to Main Menu</a></p>



Height of Soccer Players (in)



Height of Basketball Players (in)

In looking at the distribution of the data, Jason observes that there is some overlap between the two data sets. Some players on both teams have players between 73 and 78 inches tall. Jason decides to use the mean and mean absolute deviation to compare the data sets.

The mean height of the basketball players is 79.75 inches as compared to the mean height of the soccer players at 72.07 inches, a difference of 7.68 inches.

The mean absolute deviation (MAD) is calculated by taking the mean of the absolute deviations for each data point. The difference between each data point and the mean is recorded in the second column of the table. The difference between each data point and the mean is recorded in the second column of the table. Jason used rounded values (80 inches for the mean height of basketball players and 72 inches for the mean height of soccer players) to find the differences. The absolute deviation, absolute value of the deviation, is recorded in the third column. The absolute deviations are summed and divided by the number of data points in the set.

The mean absolute deviation is 2.14 inches for the basketball players and 2.53 for the soccer players. These values indicate moderate variation in both data sets.

*Solution:*

There is slightly more variability in the height of the soccer players. The difference between the heights of the teams (7.68) is approximately 3 times the variability of the data sets ( $7.68 \div 2.53 = 3.04$ ;  $7.68 \div 2.14 = 3.59$ ).

[Return to Main Menu](#)

**Soccer Players (n = 29)**

Height (in)	Deviation from Mean (in)	Absolute Deviation (in)
65	-7	7
67	-5	5
69	-3	3
69	-3	3
69	-3	3
70	-2	2
70	-2	2
71	-1	1
71	-1	1
71	-1	1
72	0	0
72	0	0
72	0	0
72	0	0
73	+1	1
73	+1	1
73	+1	1
73	+1	1
73	+1	1
74	+2	2
74	+2	2
74	+2	2
74	+2	2
76	+4	4
76	+4	4
76	+4	4
78	+6	6
$\Sigma = 2090$		$\Sigma = 62$

**Basketball Players (n = 16)**

Height (in)	Deviation from Mean (in)	Absolute Deviation (in)
73	-7	7
75	-5	5
76	-4	4
78	-2	2
78	-2	2
79	-1	1
79	-1	1
80	0	0
80	0	0
81	+1	1
81	+1	1
82	+2	2
82	+2	2
84	+4	4
84	+4	4
84	+4	4
$\Sigma = 1276$		$\Sigma = 40$

Mean =  $2090 \div 29 = 72$  inches  
 MAD =  $62 \div 29 = 2.14$  inches

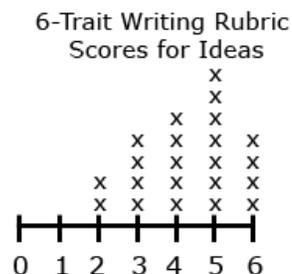
Mean =  $1276 \div 16 = 80$  inches  
 MAD =  $40 \div 16 = 2.53$  inches

[Return to Main Menu](#)

**RESOURCES** Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. *For example, decide whether the words in a chapter of a seventh-grade science book are generally longer than the words in a chapter of a fourth-grade science book.*

**7.SP.4** Students compare two sets of data using measures of center (mean and median) and variability (MAD and IQR).

Showing the two graphs vertically rather than side by side helps students make comparisons. For example, students would be able to see from the display of the two graphs that the ideas scores are generally higher than the organization scores. One observation students might make is that the scores for organization are clustered around a score of 3 whereas the scores for ideas are clustered around a score of 5.



**Example 1:**

The two data sets below depict random samples of the management salaries in two companies. Based on the salaries below which measure of center will provide the most accurate estimation of the salaries for each company?

- Company A: 1.2 million, 242,000, 265,500, 140,000, 281,000, 265,000, 211,000
- Company B: 5 million, 154,000, 250,000, 250,000, 200,000, 160,000, 190,000

**Solution:**

The median would be the most accurate measure since both companies have one value in the million that is far from the other values and would affect the mean.

[Return to Main Menu](#)

## Progression Chart

	5 <sup>th</sup> Grade	6 <sup>th</sup> Grade	7 <sup>th</sup> Grade
<b>Numbers &amp; Base Ten, Numbers &amp; Operations with Fractions, &amp; Geometry</b>	<p>Applying powers of 10 to place value &amp; multiplication</p> <p>Read, compare &amp; round decimals to the thousands</p> <p>Fluently multiply multi-digit whole numbers</p> <p>Find whole number quotients up to 4 digits dividend &amp; 2 digit divisor</p> <p>Add, subtract, multiply &amp; divide decimals to the thousandths</p> <p>Add &amp; subtract fractions with like &amp; unlike denominators &amp; apply to word problems</p> <p>Multiply &amp; divide fractions by fractions &amp; fractions by whole numbers &amp; apply to word problems</p> <p>Graphing ordered pairs in quadrant #1</p>	<b>Number Sense</b>	<p>Operations with integers (to include understanding of additive inverse)</p> <p>Computing with rational numbers (to include negative fractions &amp; decimals &amp; to include complex fractions)</p> <p>Converting fractions to decimals &amp; vice versa (NOT repeating decimals to fractions)</p> <p>Apply order of operations to solve real world &amp; math problems.</p>
<b>Measurement &amp; Data</b>	<p>Convert standard measurement units</p>	<b>6 &amp; 7 – Ratio &amp; Proportional Relations</b>	<p>Unit Rates with complex fractions</p> <p>Proportionality – table, graph, equation, context</p> <p>Proportional relationships &amp; percents with proportions</p>
		<p>Compare &amp; order integers, positive fractions &amp; decimals, and whole numbers (to include absolute value)</p> <p>Fluently perform all four operations with fractions, decimals, and whole numbers (NOT integers) with &amp; without context.</p> <p>Find GCF</p> <p>Using vertical &amp; horizontal number lines to find distance.</p> <p>Graphing points on full coordinate plane.</p>	
		<p>Ratio Tables</p> <p>Unit Rates &amp; unit pricing</p> <p>Concept of &amp; basic computation with % using bar models</p> <p>Convert measurement units</p>	

[Return to Main Menu](#)

## Progression Chart (continued)

	5 <sup>th</sup> Grade	6 <sup>th</sup> Grade	7 <sup>th</sup> Grade
<b>Measurement &amp; Data &amp; Geometry</b>	<p>Concept of volume introduced</p> <p>Find volume of rectangular prism</p> <p>Find volume of composite figures made of rectangular prisms</p> <p>Classify two-dimensional figures based on properties &amp; attributes</p> <p>Graphing ordered pairs in quadrant 1 and drawing conclusions about resulting figures</p>	<b>Geometry</b>	<p>Scale drawings</p> <p>Area &amp; circumference of a circle</p> <p>Area of composite figures</p> <p>Solve problems with supplementary, complementary, vertical and adjacent angles (NOT parallel lines cut by transversal)</p> <p>Volume &amp; Surface area of right prisms &amp; pyramids. (NOT cylinders, spheres &amp; cones)</p>
<b>Operations &amp; Algebraic Thinking</b>	<p>Order of operations with grouping symbols (non-nested)</p> <p>Writing verbal expressions to describe numerical operations</p> <p>Create &amp; compare tables &amp; graphs of 2 number patterns described by 2 rules</p>	<b>Expressions &amp; Equations</b>	<p>Simplify algebraic expressions with integers and with other rational numbers.</p> <p>Solve multi-step equations with variables on one side of = sign.</p> <p>Solve 2 step inequalities, graph &amp; interpret solution in context.</p> <p>Problem solve from context using multiple operations with positive &amp; negative rational numbers as integer, decimal, fraction, %, and whole #.</p>
<b>Measurement &amp; Data</b>	<p>Create line plots with unit fractions as scale</p>	<b>Statistics &amp; Probability</b>	<p>Sampling &amp; inferencing</p> <p>Comparing measures of variability &amp; center of two 1 variable (univariate) data sets</p> <p>Probability models &amp; calculations - simple &amp; compound</p>

[Return to Main Menu](#)

## EOG Weighted Distribution

Grade 6 Math		Number of Items Per Standard
Ratios and Proportional Relationships	6.RP.1	–
	6.RP.2	–
	6.RP.3	7
The Number System	6.NS.1	3
	6.NS.2	–
	6.NS.3	5-6
	6.NS.4	1
	6.NS.5	–
	6.NS.6	1
	6.NS.7	2-3
	6.NS.8	2
Expressions and Equations	6.EE.1	2
	6.EE.2	2
	6.EE.3	4
	6.EE.4	–
	6.EE.5	–
	6.EE.6	2
	6.EE.7	3
	6.EE.8	1
	6.EE.9	1
Geometry	6.G.1	2
	6.G.2	2
	6.G.3	2
	6.G.4	2
Statistics and Probability	6.SP.1	–
	6.SP.2	–
	6.SP.3	–
	6.SP.4	2
	6.SP.5	3

### EOG PERCENTAGES



Domain	Grade 6	Grade 7	Grade 8
Ratios and Proportional Relationships	12–17%	22–27%	NA
The Number System	27–32%	7–12%	2–7%
Expressions and Equations	27–32%	22–27%	27–32%
Functions	NA	NA	22–27%
Geometry	12–17%	22–27%	20–25%
Statistics and Probability	7–12%	12–17%	15–20%
<b>Total</b>	<b>100%</b>	<b>100%</b>	<b>100%</b>

[Return to Main Menu](#)

### ESSENTIAL QUESTIONS

- What is the purpose of division? What does it really mean?
- What does a remainder mean when dividing?
- How does a whole number remainder relate to its fraction and decimal form?
- How are operations with decimals similar and different from whole numbers?
- How can estimation and rounding be used with decimal operations?
- How can you use fractions and percents to more efficiently compute with decimals?
- How is the GCF related to the distributive property?
- How can fraction strips and bar models be used to make sense of division of fractions problems?
- How can you use estimation to help make sense of problems involving multiplication and division of fractions?
- How do you know which fraction is the divisor and which is the dividend in a word problem?
- Does a product or quotient always have to be fully simplified?
- What is absolute value?
- What are the similarities and differences between positive and negative numbers?
- How do you know if one integer is smaller or larger than another?

### ACADEMIC VOCABULARY

**Reciprocal, Multiplicative Inverses, Visual Fraction Model, Multi-digit, Greatest Common Factor, Least Common Multiple, Prime Numbers, Composite Numbers, Relatively Prime, Factors, Multiples, Distributive Property, Prime Factorization, Rational Numbers, Opposites, Absolute Value, Greater Than,  $>$ , Less Than,  $<$ , Greater Than or Equal To,  $\geq$ , Less Than or Equal To,  $\leq$ , Origin, Quadrants, Coordinate Plane, Ordered Pairs,  $x$ -axis,  $y$ -axis, Coordinates**

**[Return to Main Menu](#)**

## 2<sup>nd</sup> Nine Weeks

## Ratios and Proportional Relationships

### ESSENTIAL QUESTIONS

- What is the difference between part-to-whole ratios and part-to-part ratios?
- How are ratios and fractions alike and different?
- How are measurement conversions related to ratios?
- What is a tape diagram and how can it be used to solve ratio problems?
- What is a unit rate?
- How are a ratio and rate related?
- How are fractions, decimals and percents related?
- How does a table and graph help explain rate relationship?

#### ACADEMIC VOCABULARY

Ratios	Tape diagram	Double number line
Customary U.S.	Metric System	Scale drawing
Equivalent ratios	Rate	Unit Rate
Percent	Bar model	Part-to-part Part-to-whole

## 3<sup>rd</sup> Nine Weeks

## Geometry / Statistics and Probability

### ESSENTIAL QUESTIONS

- How do you find the horizontal or vertical distance between 2 points in the coordinate plane?
- What is the difference between an independent and dependent variable?
- How are the independent and dependent variables organized on a coordinate plane?
- Should all data be graphed with a line? Why or why not?
- How is the dependent variable impacted when the independent variable changes?
- How are the four quadrants in the coordinate plane similar and different?
- How do you know when two points represent a reflection across the x or y-axis?
- How is the area of a rectangle related to the area of a triangle?
- What shapes compose a triangle?
- How are a rectangle and triangle related?
- How can you decompose a shape to find its area?
- How can you tell the difference between a statistical question and one that is not?
- What measure is the most affective when analyzing a set of data?
- How can outliers skew a set of data?
- Which type of display best represents a set of data?
- How can each measure of center be used to describe data?
- What does the variation of data tell you?
- What measure is the most affective when analyzing a set of data?
- How can outliers skew a set of data?
- What is the difference in a histogram and box plot?
- Is the Mean a sufficient value for summarizing data?
- How does the Mean Absolute Deviation describe variability of data?

#### ACADEMIC VOCABULARY

Area, Surface Area, Volume, Decomposing, Edges,  
Dimensions, Net, Vertices, Face, Base, Height,  
Trapezoid, Isosceles, Right Triangle, Quadrilateral,  
Rectangles, Squares, Parallelograms, Trapezoids,  
Rhombi, Kites, Right Rectangular Prism, Diagonal,  
Statistics, Data, Variability, Distribution, Dot Plot,  
Histograms, Box Plots, Median, Mean

[Return to Main Menu](#)

## ESSENTIAL QUESTIONS

- When simplifying an expression with multiple operations, how do you know what operation to do first?
- What is the difference between multiplication and exponents?
- How can properties of operations create equivalent expressions?
- How do you know if two expressions are equivalent?
- When using the Distributive Property, what terms are the factors?
- What is the difference between an expression and an equation?
- What are the similarities and differences between equations and inequalities?
- How is the meaning of a variable different in an equation vs. an inequality?
- What are the different ways to solve an equation or inequality?
- What does the equal sign mean in an equation?
- What does the inequality sign mean in an inequality?

## ACADEMIC VOCABULARY

**Exponents, Base, Numerical Expressions, Algebraic Expressions, Evaluate, Sum, Term, Product, Factor, Quantity, Quotient, Coefficient, Constant, Like Terms, Equivalent Expressions, Variables, Inequalities, Equations, Greater Than,  $>$ , Less Than,  $<$ , Greater Than or Equal To,  $\geq$ , Less Than or Equal To,  $\leq$ , Profit, Exceed, Dependent Variables, Independent Variables, Discrete Data, Continuous Data**

[Return to Main Menu](#)

# CLICK ON THE ICONS FOR BILL OF FARE



[Return to Main Menu](#)

## Video Links

<https://learnzillion.com/resources/57256-6th-grade-ratios-and-proportional-relationships>

<https://learnzillion.com/resources/57257-6th-grade-the-number-system>

<https://learnzillion.com/resources/57258-6th-grade-expressions-and-equations>

<https://learnzillion.com/resources/57259-6th-grade-geometry>

<https://learnzillion.com/resources/57260-6th-grade-statistics-and-probability>

<https://learnzillion.com/resources/57265-7th-grade-ratios-and-proportional-relationships>

<https://learnzillion.com/resources/57268-7th-grade-geometry>

<https://learnzillion.com/resources/57269-7th-grade-statistics-and-probability>

<https://learnzillion.com/resources/57266-7th-grade-the-number-system>

- **REV Videos** All 2 to 3 minutes in length  
Easily Downloadable

### **Dividing Fractions**

<https://onslow.rev.vbrick.com/#/videos/5c060505-15d7-4975-85c9-0eaffe3ed70b>

### **Dividing Decimals**

<https://onslow.rev.vbrick.com/#/videos/5ab0fbe6-34da-4ee4-a124-44be2ed730bc>

### **Dividing Mixed Numbers**

<https://onslow.rev.vbrick.com/#/videos/5c060505-15d7-4975-85c9-0eaffe3ed70b>

### **Mean Absolute Deviation**

<https://onslow.rev.vbrick.com/#/videos/2395949d-a56f-49e4-88a5-02e731f560ff>

### **Box & Whisker Plots**

<https://onslow.rev.vbrick.com/#/videos/5af1497a-c0ef-46cf-8205-b00defd2df71>

### **Combining Like Terms & Distributive Property**

<https://onslow.rev.vbrick.com/#/videos/d5bf0d16-123f-4fbb-a317-f8554cd85619>

### **Surface Area**

<https://onslow.rev.vbrick.com/#/videos/21b66aad-645a-4b01-bc29-84717f36b8e9>

### **Area of Triangles**

<https://onslow.rev.vbrick.com/#/videos/77382183-4b8e-4ccb-b089-c1a2107a2027>

### **Area of Trapezoids**

<https://onslow.rev.vbrick.com/#/videos/48f98449-4d0f-4aef-b404-78534226e6e0>

### **Unit Rates**

<https://onslow.rev.vbrick.com/#/videos/fd5f90e3-3db4-491f-9157-c5f30952549a>

### ➤ **Khan Academy**

<https://www.khanacademy.org/>

### ➤ **iM**

<http://www.illustrativemathematics.org/illustrations/997>

### **Integers**

<https://onslow.rev.vbrick.com/#/videos/d894bbd4-b690-411e-be27-05ef475a231a>

### **Scale Factor**

<https://onslow.rev.vbrick.com/#/videos/a4e095b1-5c58-4048-a7f0-306764ff1540>

### **Proportions Using Similar Triangles**

<https://onslow.rev.vbrick.com/#/videos/a74d116b-fa6c-4f06-9386-01888aa9ed1f>

### **Probability**

<https://onslow.rev.vbrick.com/#/videos/f9ab5472-a894-4f1c-ace5-b0981f451b6e>

### **Fractions to Decimals/Percent**

<https://onslow.rev.vbrick.com/#/videos/721fdcf-db1c-493d-ad6a-cc22cbee622e>

### **Circumference of Circles**

<https://onslow.rev.vbrick.com/#/videos/814df4c4-d6a7-47ba-9c86-88b903486677>

### **Slicing 3-D Figures**

<https://onslow.rev.vbrick.com/#/videos/06d60b69-7daf-4fdf-ac3f-26b72d506a8b>

### **Area of Circles**

<https://onslow.rev.vbrick.com/#/videos/15a15baf-9620-467c-9d33-c15e3c38b135>

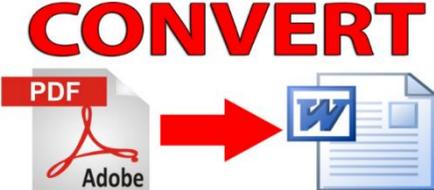
### **Percent Word Problems**

<https://onslow.rev.vbrick.com/#/videos/214c8587-08c8-42c0-a473-e07f105766ea>

### **Two-Step Equations**

<https://onslow.rev.vbrick.com/#/videos/409c589e-0035-493e-b4fd-895e870bf7ac>

[Return to Main Menu](#)

EOG Prep	Released EOG
<ul style="list-style-type: none"> <li>➤ <a href="https://parcc.pearson.com/practice-tests/math/">https://parcc.pearson.com/practice-tests/math/</a></li> <li>➤ <a href="https://cuacs8.mck.ncsu.edu/mathsampleitems/main.html">https://cuacs8.mck.ncsu.edu/mathsampleitems/main.html</a></li> </ul>	<ul style="list-style-type: none"> <li>➤ <a href="http://www.dpi.state.nc.us/docs/accountability/testing/releasedforms/g6mathpp.pdf">http://www.dpi.state.nc.us/docs/accountability/testing/releasedforms/g6mathpp.pdf</a></li> <li>➤ <a href="http://www.dpi.state.nc.us/docs/accountability/testing/releasedforms/g7mathpp.pdf">http://www.dpi.state.nc.us/docs/accountability/testing/releasedforms/g7mathpp.pdf</a></li> </ul>
Assessment Options	STEM – Project Based Learning
<ul style="list-style-type: none"> <li>➤ <b>EDMENTUM</b> <a href="http://www.edmentum.com/product-login">http://www.edmentum.com/product-login</a></li> <li>➤ <a href="https://goformative.com/">https://goformative.com/</a></li> <li>➤ <a href="https://kahoot.it/#/">https://kahoot.it/#/</a></li> <li>➤ <a href="https://quizizz.com/">https://quizizz.com/</a></li> <li>➤ <a href="https://quizlet.com/">https://quizlet.com/</a></li> <li>➤ <a href="https://www.tenmarks.com/login">https://www.tenmarks.com/login</a></li> <li>➤ <a href="https://www.assistments.org/">https://www.assistments.org/</a></li> <li>➤ <a href="http://6thgradeschoolnetassessments.weebly.com/home.html">http://6thgradeschoolnetassessments.weebly.com/home.html</a></li> <li>➤ <a href="http://7thgradeschoolnetassessments.weebly.com/">http://7thgradeschoolnetassessments.weebly.com/</a></li> </ul> 	<ul style="list-style-type: none"> <li>• <a href="http://projectbasedmath.weebly.com/">http://projectbasedmath.weebly.com/</a></li> <li>• <a href="http://www.livebinders.com/play/play?id=767726">http://www.livebinders.com/play/play?id=767726</a></li> <li>• <a href="http://bie.org/">http://bie.org/</a></li> <li>• <a href="http://www.edutopia.org/project-based-learning">http://www.edutopia.org/project-based-learning</a></li> <li>• <a href="http://www.mathalicious.com/">http://www.mathalicious.com/</a></li> </ul> <p>FREE Online PDF to Word Converter  <a href="https://www.pdfword.com/">https://www.pdfword.com/</a></p>  <p>No Password – Quick &amp; Easy!</p> <p style="text-align: right;"><b><u><a href="#">Return to Main Menu</a></u></b></p>

For more information, suggestions or input contact: Joe Sarrero [joe.sarrero@onslow.k12.nc.us](mailto:joe.sarrero@onslow.k12.nc.us)